

Chapter 16: Information Flow

- Entropy and analysis
- Non-lattice information flow policies
- Compiler-based mechanisms
- Execution-based mechanisms
- Examples

Overview

- Basics and background
 - Entropy
- Nonlattice flow policies
- Compiler-based mechanisms
- Execution-based mechanisms
- Examples
 - Security Pipeline Interface
 - Secure Network Server Mail Guard

Basics

- Bell-LaPadula Model embodies information flow policy
 - Given compartments A, B , info can flow from A to B iff $B \text{ dom } A$
- Variables x, y assigned compartments $\underline{x}, \underline{y}$ as well as values
 - If $\underline{x} = A$ and $\underline{y} = B$, and $A \text{ dom } B$, then $y := x$ allowed but not $x := y$

Entropy and Information Flow

- Idea: info flows from x to y as a result of a sequence of commands c if you can deduce information about x before c from the value in y after c
- Formally:
 - s time before execution of c , t time after
 - $H(x_s | y_t) < H(x_s | y_s)$
 - If no y at time s , then $H(x_s | y_t) < H(x_s)$

Example 1

- Command is $x := y + z$; where:
 - $0 \leq y \leq 7$, equal probability
 - $z = 1$ with prob. $1/2$, $z = 2$ or 3 with prob. $1/4$ each
- s state before command executed; t , after; so
 - $H(y_s) = H(y_t) = -8(1/8) \lg (1/8) = 3$
 - $H(z_s) = H(z_t) = -(1/2) \lg (1/2) - 2(1/4) \lg (1/4) = 1.5$
- If you know x_t , y_s can have at most 3 values, so $H(y_s | x_t) = -3(1/3) \lg (1/3) = \lg 3$

Example 2

- Command is
 - **if** $x = 1$ **then** $y := 0$ **else** $y := 1$;
- where:
 - x, y equally likely to be either 0 or 1
- $H(x_s) = 1$ as x can be either 0 or 1 with equal probability
- $H(x_s | y_t) = 0$ as if $y_t = 1$ then $x_s = 0$ and vice versa
 - Thus, $H(x_s | y_t) = 0 < 1 = H(x_s)$
- So information flowed from x to y

Implicit Flow of Information

- Information flows from x to y without an *explicit* assignment of the form $y := f(x)$
 - $f(x)$ an arithmetic expression with variable x
- Example from previous slide:
 - **if** $x = 1$ **then** $y := 0$
else $y := 1$;
- So must look for implicit flows of information to analyze program

Notation

- \underline{x} means class of x
 - In Bell-LaPadula based system, same as “label of security compartment to which x belongs”
- $\underline{x} \leq \underline{y}$ means “information can flow from an element in class of x to an element in class of y ”
 - Or, “information with a label placing it in class \underline{x} can flow into class \underline{y} ”

Information Flow Policies

Information flow policies are usually:

- reflexive
 - So information can flow freely among members of a single class
- transitive
 - So if information can flow from class 1 to class 2, and from class 2 to class 3, then information can flow from class 1 to class 3

Non-Transitive Policies

- Betty is a confident of Anne
- Cathy is a confident of Betty
 - With transitivity, information flows from Anne to Betty to Cathy
- Anne confides to Betty she is having an affair with Cathy's spouse
 - Transitivity undesirable in this case, probably

Non-Lattice Transitive Policies

- 2 faculty members co-PIs on a grant
 - Equal authority; neither can overrule the other
- Grad students report to faculty members
- Undergrads report to grad students
- Information flow relation is:
 - Reflexive and transitive
- But some elements (people) have no “least upper bound” element
 - What is it for the faculty members?

Confidentiality Policy Model

- Lattice model fails in previous 2 cases
- Generalize: policy $I = (SC_I, \leq_I, join_I)$:
 - SC_I set of security classes
 - \leq_I ordering relation on elements of SC_I
 - $join_I$ function to combine two elements of SC_I
- Example: Bell-LaPadula Model
 - SC_I set of security compartments
 - \leq_I ordering relation *dom*
 - $join_I$ function *lub*

Confinement Flow Model

- $(I, O, confine, \rightarrow)$
 - $I = (SC_I, \leq_I, join_I)$
 - O set of entities
 - $\rightarrow: O \times O$ with $(a, b) \in \rightarrow$ (written $a \rightarrow b$) iff information can flow from a to b
 - for $a \in O$, $confine(a) = (a_L, a_U) \in SC_I \times SC_I$ with $a_L \leq_I a_U$
 - Interpretation: for $a \in O$, if $x \leq_I a_U$, info can flow from x to a , and if $a_L \leq_I x$, info can flow from a to x
 - So a_L lowest classification of info allowed to flow out of a , and a_U highest classification of info allowed to flow into a

Assumptions, *etc.*

- Assumes: object can change security classes
 - So, variable can take on security class of its data
- Object x has security class \underline{x} currently
- Note transitivity *not* required
- If information can flow from a to b , then b dominates a under ordering of policy I :
$$(\forall a, b \in O)[a \rightarrow b \Rightarrow a_L \leq_I b_U]$$

Example 1

- $SC_I = \{ U, C, S, TS \}$, with $U \leq_I C$, $C \leq_I S$, and $S \leq_I TS$
- $a, b, c \in O$
 - $\text{confine}(a) = [C, C]$
 - $\text{confine}(b) = [S, S]$
 - $\text{confine}(c) = [TS, TS]$
- Secure information flows: $a \rightarrow b, a \rightarrow c, b \rightarrow c$
 - As $a_L \leq_I b_U, a_L \leq_I c_U, b_L \leq_I c_U$
 - Transitivity holds

Example 2

- SC_I, \leq_I as in Example 1
- $x, y, z \in O$
 - $\text{confine}(x) = [C, C]$
 - $\text{confine}(y) = [S, S]$
 - $\text{confine}(z) = [C, TS]$
- Secure information flows: $x \rightarrow y, x \rightarrow z, y \rightarrow z, z \rightarrow x, z \rightarrow y$
 - As $x_L \leq_I y_U, x_L \leq_I z_U, y_L \leq_I z_U, z_L \leq_I x_U, z_L \leq_I y_U$
 - Transitivity does not hold
 - $y \rightarrow z$ and $z \rightarrow x$, but $y \rightarrow x$ is false, because $y_L \leq_I x_U$ is false

Transitive Non-Lattice Policies

- $Q = (S_Q, \leq_Q)$ is a *quasi-ordered set* when \leq_Q is transitive and reflexive over S_Q
- How to handle information flow?
 - Define a partially ordered set containing quasi-ordered set
 - Add least upper bound, greatest lower bound to partially ordered set
 - It's a lattice, so apply lattice rules!

In Detail ...

- $\forall x \in S_Q$: let $f(x) = \{ y \mid y \in S_Q \wedge y \leq_Q x \}$
 - Define $S_{QP} = \{ f(x) \mid x \in S_Q \}$
 - Define $\leq_{QP} = \{ (x, y) \mid x, y \in S_Q \wedge x \subseteq y \}$
 - S_{QP} partially ordered set under \leq_{QP}
 - f preserves order, so $y \leq_Q x$ iff $f(x) \leq_{QP} f(y)$
- Add upper, lower bounds
 - $S_{QP}' = S_{QP} \cup \{ S_Q, \emptyset \}$
 - Upper bound $ub(x, y) = \{ z \mid z \in S_{QP} \wedge x \subseteq z \wedge y \subseteq z \}$
 - Least upper bound $lub(x, y) = \bigcap ub(x, y)$
 - Lower bound, greatest lower bound defined analogously

And the Policy Is ...

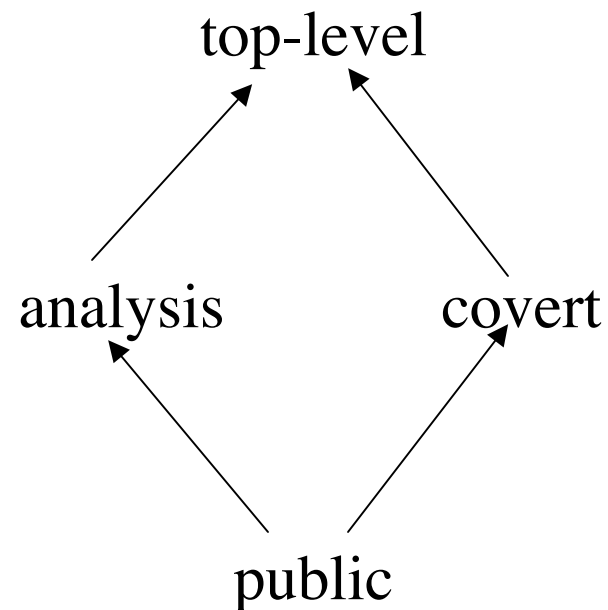
- Now $(S_{QP'}, \leq_{QP})$ is lattice
- Information flow policy on quasi-ordered set emulates that of this lattice!

Nontransitive Flow Policies

- Government agency information flow policy (on next slide)
- Entities public relations officers PRO, analysts A, spymasters S
 - $\text{confine}(\text{PRO}) = \{ \text{public, analysis} \}$
 - $\text{confine}(A) = \{ \text{analysis, top-level} \}$
 - $\text{confine}(S) = \{ \text{covert, top-level} \}$

Information Flow

- By confinement flow model:
 - $PRO \leq A, A \leq PRO$
 - $PRO \leq S$
 - $A \leq S, S \leq A$
- Data *cannot* flow to public relations officers; not transitive
 - $S \leq A, A \leq PRO$
 - $S \leq PRO$ is *false*



Transforming Into Lattice

- Rough idea: apply a special mapping to generate a subset of the power set of the set of classes
 - Done so this set is partially ordered
 - Means it can be transformed into a lattice
- Can show this mapping preserves ordering relation
 - So it preserves non-orderings and non-transitivity of elements corresponding to those of original set

Dual Mapping

- $R = (SC_R, \leq_R, join_R)$ reflexive info flow policy
- $P = (S_P, \leq_P)$ ordered set
 - Define *dual mapping* functions $l_R, h_R: SC_R \rightarrow S_P$
 - $l_R(x) = \{ x \}$
 - $h_R(x) = \{ y \mid y \in SC_R \wedge y \leq_R x \}$
 - S_P contains subsets of SC_R ; \leq_P subset relation
 - Dual mapping function *order preserving* iff
$$(\forall a, b \in SC_R) [a \leq_R b \Leftrightarrow l_R(a) \leq_P h_R(b)]$$

Theorem

Dual mapping from reflexive info flow policy R to ordered set P order-preserving

Proof sketch: all notation as before

(\Rightarrow) Let $a \leq_R b$. Then $a \in l_R(a)$, $a \in h_R(b)$, so $l_R(a) \subseteq h_R(b)$, or $l_R(a) \leq_P h_R(b)$

(\Leftarrow) Let $l_R(a) \leq_P h_R(b)$. Then $l_R(a) \subseteq h_R(b)$.

But $l_R(a) = \{ a \}$, so $a \in h_R(b)$, giving $a \leq_R b$

Info Flow Requirements

- Interpretation: let $confine(x) = \{ \underline{x}_L, \underline{x}_U \}$, consider class \underline{y}
 - Information can flow from x to element of \underline{y} iff $\underline{x}_L \leq_R \underline{y}$, or $l_R(\underline{x}_L) \subseteq h_R(\underline{y})$
 - Information can flow from element of \underline{y} to x iff $\underline{y} \leq_R \underline{x}_U$, or $l_R(\underline{y}) \subseteq h_R(\underline{x}_U)$

Revisit Government Example

- Information flow policy is R
- Flow relationships among classes are:

public \leq_R public

public \leq_R analysis

public \leq_R covert

public \leq_R top-level

analysis \leq_R top-level

analysis \leq_R analysis

covert \leq_R covert

covert \leq_R top-level

top-level \leq_R top-level

Dual Mapping of R

- Elements l_R, h_R :

$$l_R(\text{public}) = \{ \text{public} \}$$

$$h_R(\text{public}) = \{ \text{public} \}$$

$$l_R(\text{analysis}) = \{ \text{analysis} \}$$

$$h_R(\text{analysis}) = \{ \text{public}, \text{analysis} \}$$

$$l_R(\text{covert}) = \{ \text{covert} \}$$

$$h_R(\text{covert}) = \{ \text{public}, \text{covert} \}$$

$$l_R(\text{top-level}) = \{ \text{top-level} \}$$

$$h_R(\text{top-level}) = \{ \text{public}, \text{analysis}, \text{covert}, \text{top-level} \}$$

confine

- Let p be entity of type PRO, a of type A, s of type S
- In terms of P (not R), we get:
 - $confine(p) = [\{ public \}, \{ public, analysis \}]$
 - $confine(a) = [\{ analysis \},$
 $\{ public, analysis, covert, top-level \}]$
 - $confine(s) = [\{ covert \},$
 $\{ public, analysis, covert, top-level \}]$

And the Flow Relations Are ...

- $p \rightarrow a$ as $l_R(p) \subseteq h_R(a)$
 - $l_R(p) = \{ \text{public} \}$
 - $h_R(a) = \{ \text{public, analysis, covert, top-level} \}$
- Similarly: $a \rightarrow p, p \rightarrow s, a \rightarrow s, s \rightarrow a$
- **But** $s \rightarrow p$ is false as $l_R(s) \not\subseteq h_R(p)$
 - $l_R(s) = \{ \text{covert} \}$
 - $h_R(p) = \{ \text{public, analysis} \}$

Analysis

- (S_P, \leq_P) is a lattice, so it can be analyzed like a lattice policy
- Dual mapping preserves ordering, hence non-ordering and non-transitivity, of original policy
 - So results of analysis of (S_P, \leq_P) can be mapped back into $(SC_R, \leq_R, join_R)$

Compiler-Based Mechanisms

- Detect unauthorized information flows in a program during compilation
- Analysis not precise, but secure
 - If a flow *could* violate policy (but may not), it is unauthorized
 - No unauthorized path along which information could flow remains undetected
- Set of statements *certified* with respect to information flow policy if flows in set of statements do not violate that policy

Example

```
if  $x = 1$  then  $y := a;$   
else  $y := b;$ 
```

- Info flows from x and a to y , or from x and b to y
- Certified only if $\underline{x} \leq \underline{y}$ and $\underline{a} \leq \underline{y}$ and $\underline{b} \leq \underline{y}$
 - Note flows for *both* branches must be true unless compiler can determine that one branch will *never* be taken

Declarations

- Notation:

$x: \mathbf{int\ class\ \{ A, B \}}$

means x is an integer variable with security class at least $lub\{ A, B \}$, so $lub\{ A, B \} \leq \underline{x}$

- Distinguished classes *Low*, *High*
 - Constants are always *Low*

Input Parameters

- Parameters through which data passed into procedure
- Class of parameter is class of actual argument

i_p : **type class** { i_p }

Output Parameters

- Parameters through which data passed out of procedure
 - If data passed in, called input/output parameter
- As information can flow from input parameters to output parameters, class must include this:

O_p : **type class** { r_1 , ..., r_n }

where r_i is class of i th input or input/output argument

Example

```
proc sum(x: int class { A };  
    var out: int class { A, B });  
begin  
    out := out + x;  
end;
```

- Require $\underline{x} \leq \underline{out}$ and $\underline{out} \leq \underline{out}$

Array Elements

- Information flowing out:

$$\dots := a[i]$$

Value of i , $a[i]$ both affect result, so class is $\text{lub}\{ \underline{a[i]}, \underline{i} \}$

- Information flowing in:

$$a[i] := \dots$$

- Only value of $a[i]$ affected, so class is $\underline{a[i]}$

Assignment Statements

$x := y + z;$

- Information flows from y, z to x , so this requires $\text{lub}\{ \underline{y}, \underline{z} \} \leq \underline{x}$

More generally:

$y := f(x_1, \dots, x_n)$

- the relation $\text{lub}\{ \underline{x}_1, \dots, \underline{x}_n \} \leq \underline{y}$ must hold

Compound Statements

$x := y + z; a := b * c - x;$

- First statement: $\text{lub}\{ \underline{y}, \underline{z} \} \leq \underline{x}$
- Second statement: $\text{lub}\{ \underline{b}, \underline{c}, \underline{x} \} \leq \underline{a}$
- So, both must hold (i.e., be secure)

More generally:

$S_1; \dots; S_n;$

- Each individual S_i must be secure

Conditional Statements

`if $x + y < z$ then $a := b$ else $d := b * c - x$; end`

- The statement executed reveals information about x, y, z , so $\text{lub}\{ \underline{x}, \underline{y}, \underline{z} \} \leq \text{glb}\{ \underline{a}, \underline{d} \}$

More generally:

`if $f(x_1, \dots, x_n)$ then S_1 else S_2 ; end`

- S_1, S_2 must be secure
- $\text{lub}\{ \underline{x}_1, \dots, \underline{x}_n \} \leq$
 $\text{glb}\{ \underline{y} \mid y \text{ target of assignment in } S_1, S_2 \}$

Iterative Statements

```
while  $i < n$  do begin  $a[i] := b[i]; i := i + 1;$   
end
```

- Same ideas as for “if”, but must terminate

More generally:

```
while  $f(x_1, \dots, x_n)$  do  $S;$ 
```

- Loop must terminate;
- S must be secure
- $\text{lub}\{ \underline{x}_1, \dots, \underline{x}_n \} \leq$
 $\text{glb}\{ \underline{y} \mid \underline{y} \text{ target of assignment in } S \}$

Iterative Statements

while $i < n$ do begin $a[i] := b[i]; i := i + 1;$ end

- Same ideas as for “if”, but must terminate

More generally:

while $f(x_1, \dots, x_n)$ do $S;$

- Loop must terminate;
- S must be secure
- $\text{lub}\{ \underline{x}_1, \dots, \underline{x}_n \} \leq$
 $\text{glb}\{ \underline{y} \mid y \text{ target of assignment in } S \}$

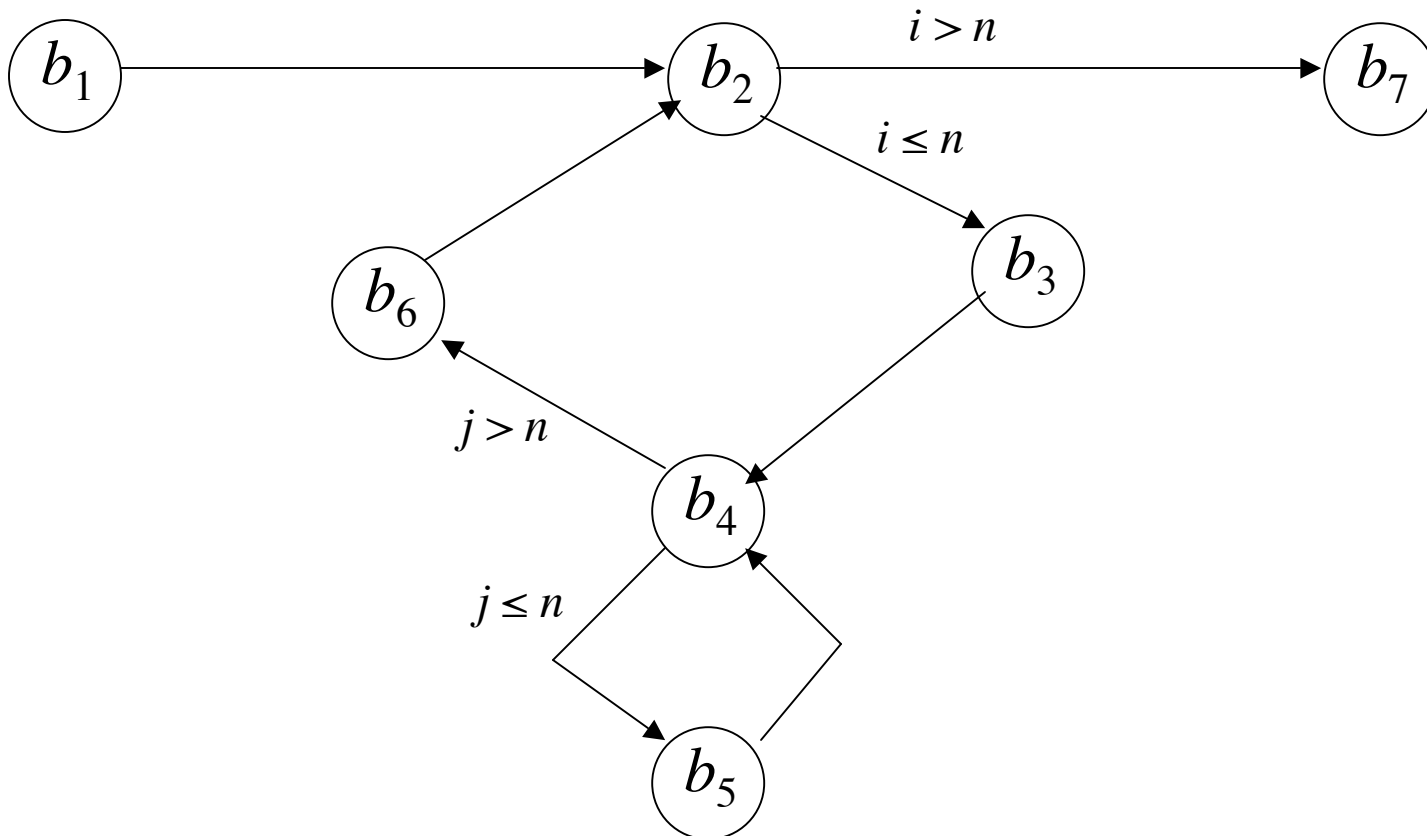
Goto Statements

- No assignments
 - Hence no explicit flows
- Need to detect implicit flows
- *Basic block* is sequence of statements that have one entry point and one exit point
 - Control in block *always* flows from entry point to exit point

Example Program

```
proc tm(x: array[1..10][1..10] of int class {x};
      var y: array[1..10][1..10] of int class {y});
var i, j: int {i};
begin
  b1 i := 1;
  b2 L2:   if i > 10 goto L7;
  b3 j := 1;
  b4 L4:   if j > 10 then goto L6;
  b5      y[j][i] := x[i][j]; j := j + 1; goto L4;
  b6 L6:   i := i + 1; goto L2;
  b7 L7:
end;
```

Flow of Control



IFDs

- Idea: when two paths out of basic block, implicit flow occurs
 - Because information says *which* path to take
- When paths converge, either:
 - Implicit flow becomes irrelevant; or
 - Implicit flow becomes explicit
- *Immediate forward dominator* of basic block b (written $\text{IFD}(b)$) is first basic block lying on all paths of execution passing through b

IFD Example

- In previous procedure:
 - $\text{IFD}(b_1) = b_2$ one path
 - $\text{IFD}(b_2) = b_7$ $b_2 \rightarrow b_7$ or $b_2 \rightarrow b_3 \rightarrow b_6 \rightarrow b_2 \rightarrow b_7$
 - $\text{IFD}(b_3) = b_4$ one path
 - $\text{IFD}(b_4) = b_6$ $b_4 \rightarrow b_6$ or $b_4 \rightarrow b_5 \rightarrow b_6$
 - $\text{IFD}(b_5) = b_4$ one path
 - $\text{IFD}(b_6) = b_2$ one path

Requirements

- B_i is set of basic blocks along an execution path from b_i to $\text{IFD}(b_i)$
 - Analogous to statements in conditional statement
- x_{i1}, \dots, x_{in} variables in expression selecting which execution path containing basic blocks in B_i used
 - Analogous to conditional expression
- Requirements for secure:
 - All statements in each basic blocks are secure
 - $\text{lub}\{ \underline{x}_{i1}, \dots, \underline{x}_{in} \} \leq$
 $\text{glb}\{ \underline{y} \mid y \text{ target of assignment in } B_i \}$

Example of Requirements

- Within each basic block:

$$b_1: Low \leq \underline{i} \quad b_3: Low \leq \underline{j} \quad b_6: \text{lub}\{ Low, \underline{i} \} \leq \underline{i}$$

$$b_5: \text{lub}\{ \underline{x}[\underline{i}][\underline{j}], \underline{i}, \underline{j} \} \leq \underline{y}[\underline{j}][\underline{i}]; \text{lub}\{ Low, \underline{j} \} \leq \underline{j}$$

– Combining, $\text{lub}\{ \underline{x}[\underline{i}][\underline{j}], \underline{i}, \underline{j} \} \leq \underline{y}[\underline{j}][\underline{i}]$

– From declarations, true when $\text{lub}\{ \underline{x}, \underline{i} \} \leq \underline{y}$

- $B_2 = \{b_3, b_4, b_5, b_6\}$

– Assignments to $i, j, y[j][i]$; conditional is $i \leq 10$

– Requires $\underline{i} \leq \text{glb}\{ \underline{i}, \underline{j}, \underline{y}[\underline{j}][\underline{i}] \}$

– From declarations, true when $\underline{i} \leq \underline{y}$

Example (continued)

- $B_4 = \{ b_5 \}$
 - Assignments to j , $y[j][i]$; conditional is $j \leq 10$
 - Requires $j \leq \text{glb}\{ j, y[j][i] \}$
 - From declarations, means $i \leq y$
- Result:
 - Combine $\text{lub}\{ \underline{x}, \underline{i} \} \leq \underline{y}$; $\underline{i} \leq \underline{y}$; $\underline{i} \leq \underline{y}$
 - Requirement is $\text{lub}\{ \underline{x}, \underline{i} \} \leq \underline{y}$

Procedure Calls

$tm(a, b);$

From previous slides, to be secure, $\text{lub}\{ \underline{x}, \underline{i} \} \leq \underline{y}$ must hold

- In call, x corresponds to a , y to b
- Means that $\text{lub}\{ \underline{a}, \underline{i} \} \leq \underline{b}$, or $\underline{a} \leq \underline{b}$

More generally:

```
proc  $pn(i_1, \dots, i_m: \text{int}; \text{var } o_1, \dots, o_n: \text{int})$   
begin  $S$  end;
```

- S must be secure
- For all j and k , if $\underline{i}_j \leq \underline{o}_k$, then $\underline{x}_j \leq \underline{y}_k$
- For all j and k , if $\underline{o}_j \leq \underline{o}_k$, then $\underline{y}_j \leq \underline{y}_k$

Exceptions

```
proc copy(x: int class { x });
    var y: int class Low)
var sum: int class { x };
    z: int class Low;
begin
    y := z := sum := 0;
    while z = 0 do begin
        sum := sum + x;
        y := y + 1;
    end
end
```

Exceptions (*cont*)

- When sum overflows, integer overflow trap
 - Procedure exits
 - Value of x is MAXINT/y
 - Info flows from y to x , but $\underline{x} \leq \underline{y}$ never checked
- Need to handle exceptions explicitly
 - Idea: on integer overflow, terminate loop
`on integer_overflow_exception sum do z := 1;`
 - Now info flows from sum to z , meaning $\underline{sum} \leq \underline{z}$
 - This is false ($\underline{sum} = \{ x \}$ dominates $\underline{z} = \text{Low}$)

Infinite Loops

```
proc copy(x: int 0..1 class { x });  
    var y: int 0..1 class Low)  
  
begin  
    y := 0;  
    while x = 0 do  
        (* nothing *);  
    y := 1;  
end
```

- If $x = 0$ initially, infinite loop
- If $x = 1$ initially, terminates with y set to 1
- No explicit flows, but implicit flow from x to y

Semaphores

Use these constructs:

```
wait(x):  if x = 0 then block until x > 0; x := x - 1;  
signal(x): x := x + 1;
```

- x is semaphore, a shared variable
- Both executed atomically

Consider statement

```
wait(sem); x := x + 1;
```

- Implicit flow from *sem* to x
 - Certification must take this into account!

Flow Requirements

- Semaphores in *signal* irrelevant
 - Don't affect information flow in that process
- Statement S is a wait
 - $\text{shared}(S)$: set of shared variables read
 - Idea: information flows out of variables in $\text{shared}(S)$
 - $\text{fglb}(S)$: glb of assignment targets *following* S
 - So, requirement is $\text{shared}(S) \leq \text{fglb}(S)$
- $\text{begin } S_1; \dots S_n \text{ end}$
 - All S_i must be secure
 - For all i , $\underline{\text{shared}(S_i)} \leq \text{fglb}(S_i)$

Example

begin

$x := y + z;$ $(* S_1 *)$

$\text{wait}(sem);$ $(* S_2 *)$

$a := b * c - x;$ $(* S_3 *)$

end

- Requirements:

- $\text{lub}\{ \underline{y}, \underline{z} \} \leq \underline{x}$

- $\text{lub}\{ \underline{b}, \underline{c}, \underline{x} \} \leq \underline{a}$

- $\underline{sem} \leq \underline{a}$

- Because $\text{fglb}(S_2) = \underline{a}$ and $\text{shared}(S_2) = sem$

Concurrent Loops

- Similar, but wait in loop affects *all* statements in loop
 - Because if flow of control loops, statements in loop before wait may be executed after wait
- Requirements
 - Loop terminates
 - All statements S_1, \dots, S_n in loop secure
 - $\text{lub}\{ \underline{\text{shared}}(S_1), \dots, \underline{\text{shared}}(S_n) \} \leq \text{glb}(t_1, \dots, t_m)$
 - Where t_1, \dots, t_m are variables assigned to in loop

Loop Example

```
while  $i < n$  do begin
     $a[i] := item;$       (*  $S_1$  *)
    wait( $sem$ );          (*  $S_2$  *)
     $i := i + 1;$        (*  $S_3$  *)
end
```

- Conditions for this to be secure:
 - Loop terminates, so this condition met
 - S_1 secure if $\text{lub}\{ \underline{i}, \underline{item} \} \leq \underline{a[i]}$
 - S_2 secure if $\underline{sem} \leq \underline{i}$ and $\underline{sem} \leq \underline{a[i]}$
 - S_3 trivially secure

cobegin/coend

cobegin

$x ::= y + z; \quad (* S_1 *)$

$a ::= b * c - y; \quad (* S_2 *)$

coend

- No information flow among statements
 - For S_1 , $\text{lub}\{ \underline{y}, \underline{z} \} \leq \underline{x}$
 - For S_2 , $\text{lub}\{ \underline{b}, \underline{c}, \underline{y} \} \leq \underline{a}$
- Security requirement is both must hold
 - So this is secure if $\text{lub}\{ \underline{y}, \underline{z} \} \leq \underline{x} \wedge \text{lub}\{ \underline{b}, \underline{c}, \underline{y} \} \leq \underline{a}$

Soundness

- Above exposition intuitive
- Can be made rigorous:
 - Express flows as types
 - Equate certification to correct use of types
 - Checking for valid information flows same as checking types conform to semantics imposed by security policy

Execution-Based Mechanisms

- Detect and stop flows of information that violate policy
 - Done at run time, not compile time
- Obvious approach: check explicit flows
 - Problem: assume for security, $\underline{x} \leq \underline{y}$
 $\text{if } x = 1 \text{ then } y := a;$
 - When $x \neq 1$, $\underline{x} = \text{High}$, $\underline{y} = \text{Low}$, $\underline{a} = \text{Low}$, appears okay—but implicit flow violates condition!

Fenton's Data Mark Machine

- Each variable has an associated class
- Program counter (PC) has one too
- Idea: branches are assignments to PC, so you can treat implicit flows as explicit flows
- Stack-based machine, so everything done in terms of pushing onto and popping from a program stack

Instruction Description

- *skip* means instruction not executed
- *push*(x , \underline{x}) means push variable x and its security class \underline{x} onto program stack
- *pop*(x , \underline{x}) means pop top value and security class from program stack, assign them to variable x and its security class \underline{x} respectively

Instructions

- $x := x + 1$ (increment)
 - Same as:
`if $\underline{PC} \leq \underline{x}$ then $x := x + 1$ else skip`
- `if $x = 0$ then goto n else $x := x - 1$` (branch and save PC on stack)
 - Same as:
`if $x = 0$ then begin
 push(PC , \underline{PC}); $\underline{PC} := \text{lub}\{\underline{PC}, x\}$; $PC := n$;
end else if $\underline{PC} \leq \underline{x}$ then
 $x := x - 1$
else
 skip;`

More Instructions

- `if' $x = 0$ then goto n else $x := x - 1$`
(branch without saving PC on stack)
 - Same as:
`if $x = 0$ then`
 - `if $\underline{x} \leq \underline{PC}$ then $PC := n$ else skip`
 - `else`
 - `if $\underline{PC} \leq \underline{x}$ then $x := x - 1$ else skip`

More Instructions

- `return` (go to just after last *if*)
 - Same as:
`pop(PC, PC);`
- `halt` (stop)
 - Same as:
`if program stack empty then halt`
 - Note stack empty to prevent user obtaining information from it after halting

Example Program

```
1  if x = 0 then goto 4 else x := x - 1
2  if z = 0 then goto 6 else z := z - 1
3  halt
4  z := z - 1
5  return
6  y := y - 1
7  return
```

- Initially $x = 0$ or $x = 1$, $y = 0$, $z = 0$
- Program copies value of x to y

Example Execution

x	y	z	PC	\underline{PC}	$stack$	$check$
1	0	0	1	Low	—	
0	0	0	2	Low	—	$Low \leq \underline{x}$
0	0	0	6	\underline{z}	(3, Low)	
0	1	0	7	\underline{z}	(3, Low)	$\underline{PC} \leq y$
0	1	0	3	Low	—	

Handling Errors

- Ignore statement that causes error, but continue execution
 - If aborted or a visible exception taken, user could deduce information
 - Means errors cannot be reported unless user has clearance at least equal to that of the information causing the error

Variable Classes

- Up to now, classes fixed
 - Check relationships on assignment, etc.
- Consider variable classes
 - Fenton's Data Mark Machine does this for PC
 - On assignment of form $y := f(x_1, \dots, x_n)$, \underline{y} changed to $\text{lub}\{ \underline{x}_1, \dots, \underline{x}_n \}$
 - Need to consider implicit flows, also

Example Program

```
(* Copy value from  $x$  to  $y$ 
 * Initially,  $x$  is 0 or 1 *)
proc copy( $x$ : int class {  $x$  });
           var  $y$ : int class {  $y$  })
var  $z$ : int class variable { Low };
begin
   $y$  := 0;
   $z$  := 0;
  if  $x$  = 0 then  $z$  := 1;
  if  $z$  = 0 then  $y$  := 1;
end;
```

- \underline{z} changes when z assigned to
- Assume $\underline{y} < \underline{x}$

Analysis of Example

- $x = 0$
 - $z := 0$ sets \underline{z} to Low
 - `if $x = 0$ then $z := 1$` sets z to 1 and \underline{z} to \underline{x}
 - So on exit, $y = 0$
- $x = 1$
 - $z := 0$ sets \underline{z} to Low
 - `if $z = 0$ then $y := 1$` sets y to 1 and checks that $\text{lub}\{\text{Low}, \underline{z}\} \leq \underline{y}$
 - So on exit, $y = 1$
- Information flowed from \underline{x} to \underline{y} even though $\underline{y} < \underline{x}$

Handling This (1)

- Fenton's Data Mark Machine detects implicit flows violating certification rules

Handling This (2)

- Raise class of variables assigned to in conditionals even when branch not taken
- Also, verify information flow requirements even when branch not taken
- Example:
 - In `if $x = 0$ then $z := 1$` , z raised to x whether or not $x = 0$
 - Certification check in next statement, that $z \leq \underline{y}$, fails, as $z = \underline{x}$ from previous statement, and $\underline{y} \leq \underline{x}$

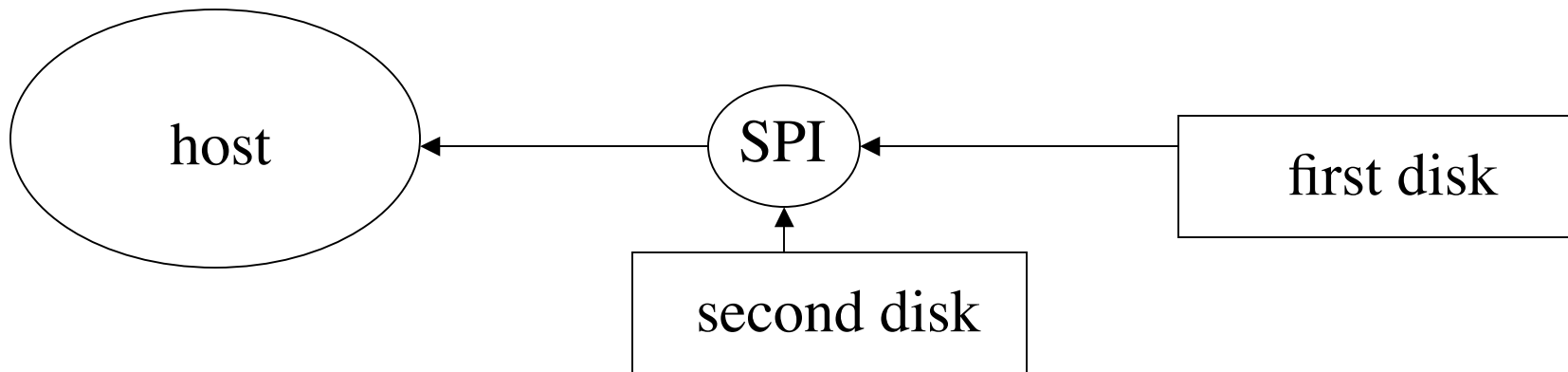
Handling This (3)

- Change classes only when explicit flows occur, but *all* flows (implicit as well as explicit) force certification checks
- Example
 - When $x = 0$, first “if” sets \underline{z} to Low then checks $\underline{x} \leq \underline{z}$
 - When $x = 1$, first “if” checks that $\underline{x} \leq \underline{z}$
 - This holds if and only if $\underline{x} = \text{Low}$
 - Not possible as $\underline{y} < \underline{x} = \text{Low}$ and there is no such class

Example Information Flow Control Systems

- Use access controls of various types to inhibit information flows
- Security Pipeline Interface
 - Analyzes data moving from host to destination
- Secure Network Server Mail Guard
 - Controls flow of data between networks that have different security classifications

Security Pipeline Interface

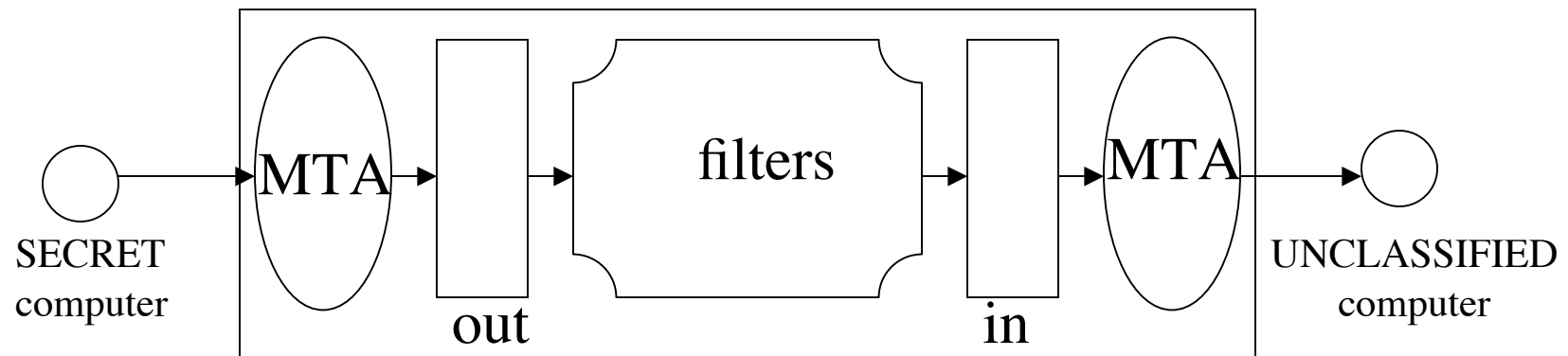


- SPI analyzes data going to, from host
 - No access to host main memory
 - Host has no control over SPI

Use

- Store files on first disk
- Store corresponding crypto checksums on second disk
- Host requests file from first disk
 - SPI retrieves file, computes crypto checksum
 - SPI retrieves file's crypto checksum from second disk
 - If a match, file is fine and forwarded to host
 - If discrepancy, file is compromised and host notified
- Integrity information flow restricted here
 - Corrupt file can be seen but will not be trusted

Secure Network Server Mail Guard (SNSMG)



- Filters analyze outgoing messages
 - Check authorization of sender
 - Sanitize message if needed (words and viruses, etc.)
- Uses type checking to enforce this
 - Incoming, outgoing messages of different type
 - Only appropriate type can be moved in or out

Key Points

- Both amount of information, direction of flow important
 - Flows can be explicit or implicit
- Analysis assumes lattice model
 - Non-lattices can be embedded in lattices
- Compiler-based checks flows at compile time
- Execution-based checks flows at run time