## Chapter 8: Basic Cryptography

- Classical Cryptography
- Public Key Cryptography
- Cryptographic Checksums

#### Overview

- Classical Cryptography
  - Cæsar cipher
  - Vigènere cipher
  - DES
- Public Key Cryptography
  - Diffie-Hellman
  - RSA
- Cryptographic Checksums
  - HMAC

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## Cryptosystem

- Quintuple ( $\mathcal{E}, \mathcal{D}, \mathcal{M}, \mathcal{K}, C$ )
  - $\mathcal{M}$  set of plaintexts
  - $\mathcal K$  set of keys
  - C set of ciphertexts
  - $\mathcal{I}$  set of encryption functions  $e: \mathcal{M} \times \mathcal{K} \rightarrow C$
  - $\mathcal{D}$  set of decryption functions  $d: C \times \mathcal{K} \rightarrow \mathcal{M}$

## Example

- Example: Cæsar cipher
  - $\mathcal{M} = \{ \text{ sequences of letters } \}$
  - $\mathcal{K} = \{ i \mid i \text{ is an integer and } 0 \le i \le 25 \}$

- 
$$\mathcal{E} = \{ E_k \mid k \in \mathcal{K} \text{ and for all letters } m, \}$$

 $E_k(m) = (m + k) \mod 26$  }

-  $\mathcal{D} = \{ D_k \mid k \in \mathcal{K} \text{ and for all letters } c,$  $D_k(c) = (26 + c - k) \mod 26 \}$ 

$$-C = \mathcal{M}$$

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#### Attacks

- Opponent whose goal is to break cryptosystem is the *adversary* 
  - Assume adversary knows algorithm used, but not key
- Three types of attacks:
  - *ciphertext only*: adversary has only ciphertext; goal is to find plaintext, possibly key
  - *known plaintext*: adversary has ciphertext, corresponding plaintext; goal is to find key
  - *chosen plaintext*: adversary may supply plaintexts and obtain corresponding ciphertext; goal is to find key

#### Basis for Attacks

- Mathematical attacks
  - Based on analysis of underlying mathematics
- Statistical attacks
  - Make assumptions about the distribution of letters, pairs of letters (digrams), triplets of letters (trigrams), *etc*.
    - Called *models of the language*
  - Examine ciphertext, correlate properties with the assumptions.

# Classical Cryptography

- Sender, receiver share common key
  - Keys may be the same, or trivial to derive from one another
  - Sometimes called *symmetric cryptography*
- Two basic types
  - Transposition ciphers
  - Substitution ciphers
  - Combinations are called *product ciphers*

## Transposition Cipher

- Rearrange letters in plaintext to produce ciphertext
- Example (Rail-Fence Cipher)
  - Plaintext is HELLO WORLD
  - Rearrange as

#### HLOOL

#### ELWRD

- Ciphertext is **HLOOL ELWRD** 

## Attacking the Cipher

- Anagramming
  - If 1-gram frequencies match English frequencies, but other *n*-gram frequencies do not, probably transposition
  - Rearrange letters to form *n*-grams with highest frequencies

## Example

- Ciphertext: HLOOLELWRD
- Frequencies of 2-grams beginning with H
  - HE 0.0305
  - HO 0.0043
  - HL, HW, HR, HD < 0.0010
- Frequencies of 2-grams ending in H
  - WH 0.0026
  - EH, LH, OH, RH, DH  $\leq 0.0002$
- Implies E follows H

### Example

• Arrange so the H and E are adjacent HE

LL

OW

#### OR

#### LD

• Read off across, then down, to get original plaintext

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## Substitution Ciphers

- Change characters in plaintext to produce ciphertext
- Example (Cæsar cipher)
  - Plaintext is HELLO WORLD
  - Change each letter to the third letter following it (X goes to A, Y to B, Z to C)
    - Key is 3, usually written as letter 'D'
  - Ciphertext is KHOOR ZRUOG

## Attacking the Cipher

- Exhaustive search
  - If the key space is small enough, try all possible keys until you find the right one
  - Cæsar cipher has 26 possible keys
- Statistical analysis
  - Compare to 1-gram model of English

#### Statistical Attack

• Compute frequency of each letter in ciphertext:

G 0.1 H 0.1 K 0.1 O 0.3 R 0.2 U 0.1 Z 0.1

- Apply 1-gram model of English
  - Frequency of characters (1-grams) in English is on next slide

#### **Character Frequencies**

a	0.080	h	0.060	n	0.070	t	0.090
b	0.015	i	0.065	0	0.080	u	0.030
c	0.030	j	0.005	p	0.020	V	0.010
d	0.040	k	0.005	q	0.002	W	0.015
e	0.130	1	0.035	r	0.065	X	0.005
f	0.020	m	0.030	S	0.060	У	0.020
g	0.015					Z	0.002

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### Statistical Analysis

- f(c) frequency of character c in ciphertext
- φ(*i*) correlation of frequency of letters in ciphertext with corresponding letters in English, assuming key is *i*

$$-\varphi(i) = \sum_{0 \le c \le 25} f(c)p(c-i) \text{ so here,}$$
  

$$\varphi(i) = 0.1p(6-i) + 0.1p(7-i) + 0.1p(10-i) + 0.3p(14-i) + 0.2p(17-i) + 0.1p(20-i) + 0.1p(25-i)$$

• p(x) is frequency of character x in English

## Correlation: $\varphi(i)$ for $0 \le i \le 25$

i	<b>φ</b> ( <i>i</i> )	i	<b>φ</b> ( <i>i</i> )	i	<b>φ</b> ( <i>i</i> )	i	<b>φ</b> ( <i>i</i> )
0	0.0482	7	0.0442	13	0.0520	19	0.0315
1	0.0364	8	0.0202	14	0.0535	20	0.0302
2	0.0410	9	0.0267	15	0.0226	21	0.0517
3	0.0575	10	0.0635	16	0.0322	22	0.0380
4	0.0252	11	0.0262	17	0.0392	23	0.0370
5	0.0190	12	0.0325	18	0.0299	24	0.0316
6	0.0660					25	0.0430

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#### The Result

- Most probable keys, based on  $\varphi$ :
  - $-i = 6, \varphi(i) = 0.0660$ 
    - plaintext EBIIL TLOLA
  - $-i = 10, \varphi(i) = 0.0635$ 
    - plaintext AXEEH PHKEW
  - $-i = 3, \varphi(i) = 0.0575$ 
    - plaintext HELLO WORLD
  - $-i = 14, \varphi(i) = 0.0535$ 
    - plaintext WTAAD LDGAS
- Only English phrase is for i = 3
  - That's the key (3 or 'D')

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### Cæsar's Problem

- Key is too short
  - Can be found by exhaustive search
  - Statistical frequencies not concealed well
    - They look too much like regular English letters
- So make it longer
  - Multiple letters in key
  - Idea is to smooth the statistical frequencies to make cryptanalysis harder

## Vigènere Cipher

- Like Cæsar cipher, but use a phrase
- Example
  - Message THE BOY HAS THE BALL
  - Key VIG
  - Encipher using Cæsar cipher for each letter:

key	VIGVIGVIGVIGVIGV
plain	THEBOYHASTHEBALL
cipher	OPKWWECIYOPKWIRG

#### Relevant Parts of Tableau

	G	I	V
A	G	I	V
В	Н	J	W
E	${f L}$	Μ	$\mathbf{Z}$
Н	N	Р	С
L	R	Т	G
0	U	W	J
S	Y	A	Ν
T	Z	В	0
Y	E	Η	Т

- Tableau shown has relevant rows, columns only
- Example encipherments:
  - key V, letter T: follow V
     column down to T row
     (giving "O")
  - Key I, letter H: follow I
     column down to H row
     (giving "P")

### Useful Terms

- *period*: length of key
  - In earlier example, period is 3
- *tableau*: table used to encipher and decipher
  - Vigènere cipher has key letters on top, plaintext letters on the left
- *polyalphabetic*: the key has several different letters
  - Cæsar cipher is monoalphabetic

## Attacking the Cipher

- Approach
  - Establish period; call it *n*
  - Break message into *n* parts, each part being enciphered using the same key letter
  - Solve each part
    - You can leverage one part from another
- We will show each step

## The Target Cipher

We want to break this cipher:
 ADQYS MIUSB OXKKT MIBHK IZOOO
 EQOOG IFBAG KAUMF VVTAA CIDTW
 MOCIO EQOOG BMBFV ZGGWP CIEKQ
 HSNEW VECNE DLAAV RWKXS VNSVP
 HCEUT QOIOF MEGJS WTPCH AJMOC
 HIUIX

#### Establish Period

- Kaskski: repetitions in the ciphertext occur when characters of the key appear over the same characters in the plaintext
- Example:

key VIGVIGVIGVIGVIGV plain THEBOYHASTHEBALL cipher <u>OPKW</u>WECIY<u>OPKW</u>IRG

Note the key and plaintext line up over the repetitions (underlined). As distance between repetitions is 9, the period is a factor of 9 (that is, 1, 3, or 9)

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### Repetitions in Example

Letters	Start	End	Distance	Factors
MI	5	15	10	2, 5
00	22	27	5	5
OEQOOG	24	54	30	2, 3, 5
FV	39	63	24	2, 2, 2, 3
AA	43	87	44	2, 2, 11
MOC	50	122	72	2, 2, 2, 3, 3
QO	56	105	49	7,7
PC	69	117	48	2, 2, 2, 2, 3
NE	77	83	6	2, 3
SV	94	97	3	3
СН	118	124	6	2, 3

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#### Estimate of Period

- OEQOOG is probably not a coincidence
  - It's too long for that
  - Period may be 1, 2, 3, 5, 6, 10, 15, or 30
- Most others (7/10) have 2 in their factors
- Almost as many (6/10) have 3 in their factors
- Begin with period of  $2 \times 3 = 6$

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#### Check on Period

- Index of coincidence is probability that two randomly chosen letters from ciphertext will be the same
- Tabulated for different periods:
  - 1 0.066 3 0.047 5 0.044
  - 2 0.052 4 0.045 10 0.041
  - Large 0.038

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## Compute IC

- IC =  $[n (n-1)]^{-1} \sum_{0 \le i \le 25} [F_i (F_i 1)]$ 
  - where *n* is length of ciphertext and  $F_i$  the number of times character *i* occurs in ciphertext
- Here, IC = 0.043
  - Indicates a key of slightly more than 5
  - A statistical measure, so it can be in error, but it agrees with the previous estimate (which was 6)

## Splitting Into Alphabets

alphabet 1: AIKHOIATTOBGEEERNEOSAI alphabet 2: DUKKEFUAWEMGKWDWSUFWJU alphabet 3: QSTIQBMAMQBWQVLKVTMTMI alphabet 4: YBMZOAFCOOFPHEAXPQEPOX alphabet 5: SOIOOGVICOVCSVASHOGCC alphabet 6: MXBOGKVDIGZINNVVCIJHH

• ICs (#1, 0.069; #2, 0.078; #3, 0.078; #4, 0.056; #5, 0.124; #6, 0.043) indicate all alphabets have period 1, except #4 and #6; assume statistics off

### Frequency Examination

#### ABCDEFGHIJKLMNOPQRSTUVWXYZ

- 1 31004011301001300112000000
- 2 1002221001301000010404000
- 3 1200000201140004013021000
- 4 2110220100001043100000211
- 5 10500021200000500030020000
- 6 0111002231101210000030101

Letter frequencies are (H high, M medium, L low):

#### HMMMHMMHHMMHHMLHHHMLLLL

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## Begin Decryption

- First matches characteristics of unshifted alphabet
- Third matches if I shifted to A
- Sixth matches if V shifted to A
- Substitute into ciphertext (bold are substitutions)

ADIYS	RIUKB	OCKKL	MI <b>GH</b> K	AZOTO
EIOOL	<b>I</b> F <b>T</b> AG	PAUEF	VATAS	CIITW
EOCNO	EIOOL	$\mathbf{B}$ M $\mathbf{T}$ FV	$\mathbf{EG}\mathbf{GOP}$	CNEKI
HS <b>SE</b> W	NECSE	D <b>D</b> AA <b>A</b>	RWCXS	ANSNP
H <b>HE</b> UL	QO <b>NO</b> F	<b>E</b> EG <b>OS</b>	WLPCM	AJEOC
MIUAX				

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#### Look For Clues

- AJE in last line suggests "are", meaning second alphabet maps A into S:
  - ALIYS RICKB OCKSL MIGHS AZOTO
  - MIOOL INTAG PACEF VATIS CIITE
  - EOCNO MIOOL BUTFV EGOOP CNESI
  - HSSEE NECSE LDAAA RECXS ANANP
  - HHECL QONON EEGOS ELPCM AREOC

#### MICAX

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## Next Alphabet

• MICAX in last line suggests "mical" (a common ending for an adjective), meaning fourth alphabet maps O into A:

ALIMS	RICKP	OCKSL	AIGHS	<b>AN</b> O <b>TO</b>
MICOL	$\mathbf{INTO}\mathbf{G}$	PACET	VATIS	QIITE
<b>EC</b> CNO	MICOL	$\mathbf{BUTT}\mathbf{V}$	EGOOD	CNESI
VSSEE	NSCSE	LDOAA	<b>RECL</b> S	ANAND
HHECL	EONON	<b>ES</b> GOS	ELDCM	<b>AREC</b> C
MICAL				

## Got It!

• QI means that U maps into I, as Q is always followed by U:

ALIME	RICKP	ACKSL	AUGHS	ANATO
MICAL	INTOS	PACET	HATIS	QUITE
ECONO	MICAL	BUTTH	EGOOD	ONESI
VESEE	NSOSE	LDOMA	RECLE	ANAND
THECL	EANON	ESSOS	ELDOM	ARECO
MICAL				

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#### One-Time Pad

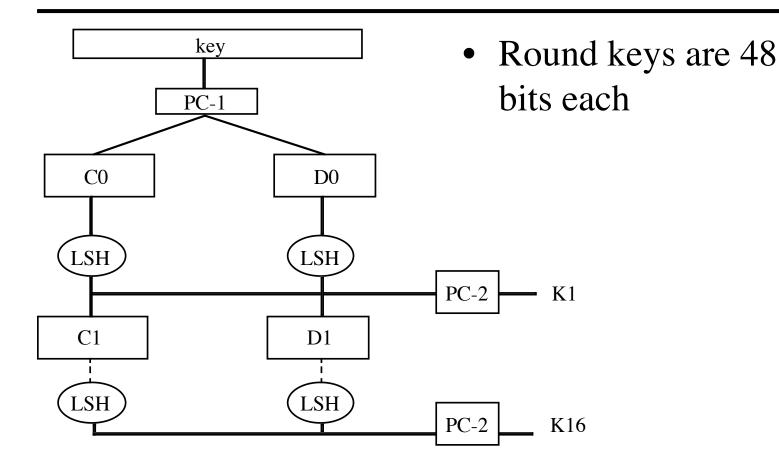
- A Vigenère cipher with a random key at least as long as the message
  - Provably unbreakable
  - Why? Look at ciphertext DXQR. Equally likely to correspond to plaintext DOIT (key AJIY) and to plaintext DONT (key AJDY) and any other 4 letters
  - Warning: keys *must* be random, or you can attack the cipher by trying to regenerate the key
    - Approximations, such as using pseudorandom number generators to generate keys, are *not* random

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#### Overview of the DES

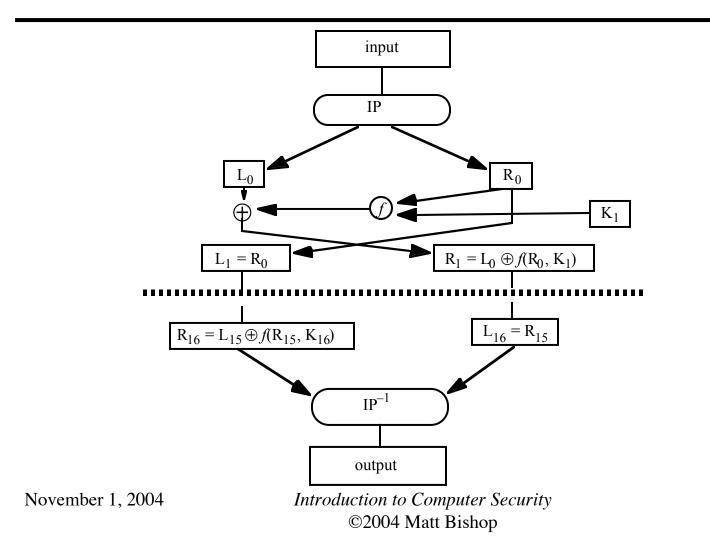
- A block cipher:
  - encrypts blocks of 64 bits using a 64 bit key
  - outputs 64 bits of ciphertext
- A product cipher
  - basic unit is the bit
  - performs both substitution and transposition (permutation) on the bits
- Cipher consists of 16 rounds (iterations) each with a round key generated from the user-supplied key

#### Generation of Round Keys



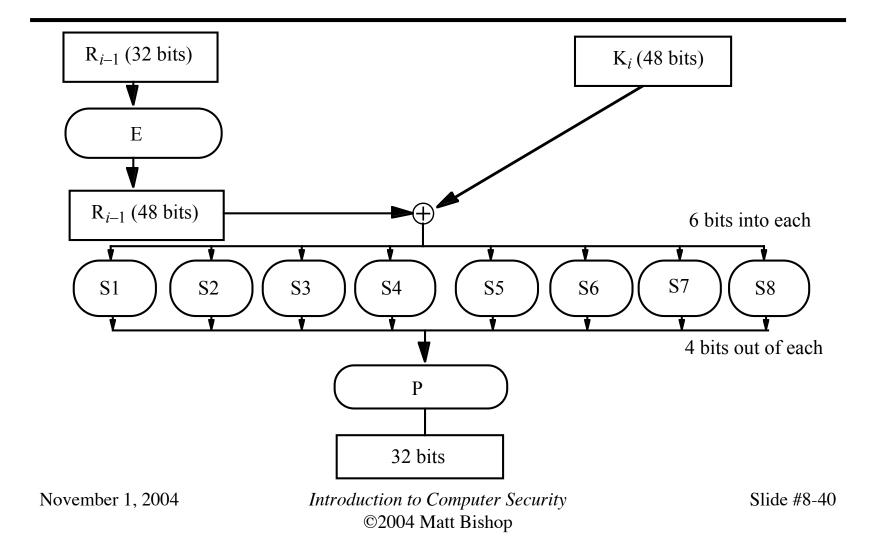
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#### Encipherment



Slide #8-39

#### The f Function



### Controversy

- Considered too weak
  - Diffie, Hellman said in a few years technology would allow DES to be broken in days
    - Design using 1999 technology published
  - Design decisions not public
    - S-boxes may have backdoors

### **Undesirable Properties**

- 4 weak keys
  - They are their own inverses
- 12 semi-weak keys
  - Each has another semi-weak key as inverse
- Complementation property
  - $\text{DES}_k(m) = c \Rightarrow \text{DES}_k(m') = c'$
- S-boxes exhibit irregular properties
  - Distribution of odd, even numbers non-random
  - Outputs of fourth box depends on input to third box

# Differential Cryptanalysis

- A chosen ciphertext attack
  - Requires 2<sup>47</sup> plaintext, ciphertext pairs
- Revealed several properties
  - Small changes in S-boxes reduce the number of pairs needed
  - Making every bit of the round keys independent does not impede attack
- Linear cryptanalysis improves result
  - Requires 2<sup>43</sup> plaintext, ciphertext pairs

#### **DES** Modes

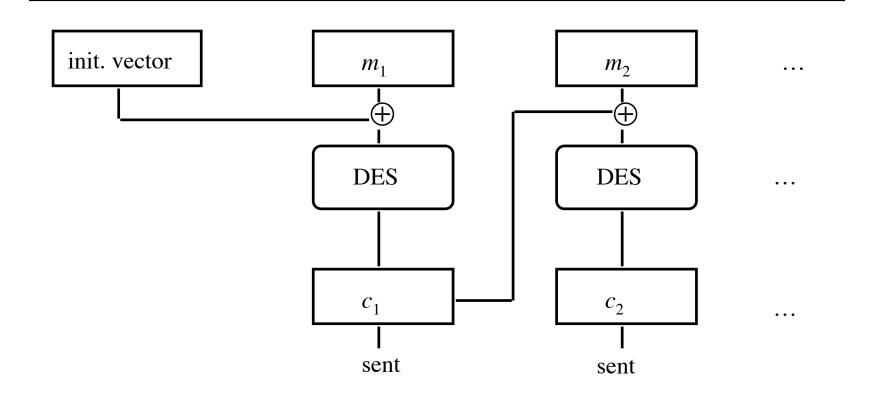
- Electronic Code Book Mode (ECB)
  - Encipher each block independently
- Cipher Block Chaining Mode (CBC)
  - Xor each block with previous ciphertext block
  - Requires an initialization vector for the first one
- Encrypt-Decrypt-Encrypt Mode (2 keys: *k*, *k'*)

 $- c = \text{DES}_k(\text{DES}_k^{-1}(\text{DES}_k(m)))$ 

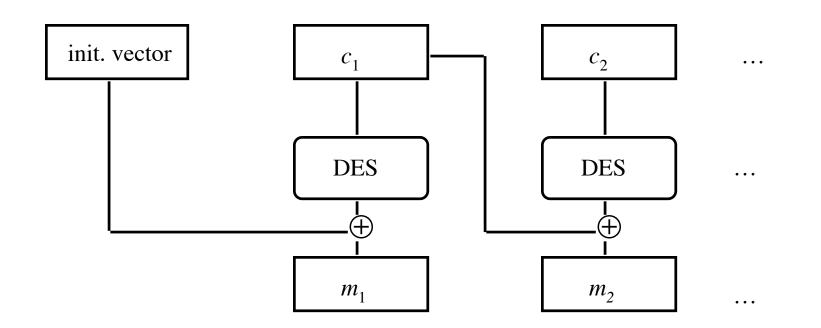
• Encrypt-Encrypt-Encrypt Mode (3 keys: k, k', k'') -  $c = DES_k(DES_{k'}(DES_{k'}(m)))$ 

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#### **CBC** Mode Encryption



#### **CBC** Mode Decryption



# Self-Healing Property

- Initial message
  - 3231343336353837 3231343336353837 3231343336353837 3231343336353837
- Received as (underlined 4c should be 4b)
  - ef7c<u>4c</u>b2b4ce6f3b f6266e3a97af0e2c 746ab9a6308f4256 33e60b451b09603d
- Which decrypts to
  - efca61e19f4836f1 323133336353837 3231343336353837 3231343336353837
  - Incorrect bytes underlined
  - Plaintext "heals" after 2 blocks

#### Current Status of DES

- Design for computer system, associated software that could break any DES-enciphered message in a few days published in 1998
- Several challenges to break DES messages solved using distributed computing
- NIST selected Rijndael as Advanced Encryption Standard, successor to DES
  - Designed to withstand attacks that were successful on DES

# Public Key Cryptography

- Two keys
  - Private key known only to individual
  - Public key available to anyone
    - Public key, private key inverses
- Idea
  - Confidentiality: encipher using public key, decipher using private key
  - Integrity/authentication: encipher using private key, decipher using public one

## Requirements

- 1. It must be computationally easy to encipher or decipher a message given the appropriate key
- 2. It must be computationally infeasible to derive the private key from the public key
- 3. It must be computationally infeasible to determine the private key from a chosen plaintext attack

## RSA

- Exponentiation cipher
- Relies on the difficulty of determining the number of numbers relatively prime to a large integer *n*

## Background

- Totient function  $\phi(n)$ 
  - Number of positive integers less than *n* and relatively prime to *n*
    - *Relatively prime* means with no factors in common with *n*
- Example:  $\phi(10) = 4$ 
  - 1, 3, 7, 9 are relatively prime to 10
- Example:  $\phi(21) = 12$ 
  - 1, 2, 4, 5, 8, 10, 11, 13, 16, 17, 19, 20 are relatively prime to 21

## Algorithm

- Choose two large prime numbers *p*, *q* 
  - Let n = pq; then  $\phi(n) = (p-1)(q-1)$
  - Choose e < n such that e is relatively prime to  $\phi(n)$ .
  - Compute *d* such that  $ed \mod \phi(n) = 1$
- Public key: (*e*, *n*); private key: *d*
- Encipher:  $c = m^e \mod n$
- Decipher:  $m = c^d \mod n$

### Example: Confidentiality

- Take p = 7, q = 11, so n = 77 and  $\phi(n) = 60$
- Alice chooses e = 17, making d = 53
- Bob wants to send Alice secret message HELLO (07 04 11 11 14)
  - $-07^{17} \mod 77 = 28$
  - $-04^{17} \mod 77 = 16$
  - $-11^{17} \mod 77 = 44$
  - $-11^{17} \mod 77 = 44$
  - $-14^{17} \mod 77 = 42$
- Bob sends 28 16 44 44 42

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## Example

- Alice receives 28 16 44 44 42
- Alice uses private key, d = 53, to decrypt message:
  - $-28^{53} \mod 77 = 07$
  - $-16^{53} \mod 77 = 04$
  - $-44^{53} \mod 77 = 11$
  - $-44^{53} \mod 77 = 11$
  - $-42^{53} \mod 77 = 14$
- Alice translates message to letters to read HELLO
  - No one else could read it, as only Alice knows her private key and that is needed for decryption

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## Example: Integrity/Authentication

- Take p = 7, q = 11, so n = 77 and  $\phi(n) = 60$
- Alice chooses e = 17, making d = 53
- Alice wants to send Bob message HELLO (07 04 11 11 14) so Bob knows it is what Alice sent (no changes in transit, and authenticated)
  - $07^{53} \mod 77 = 35$
  - $04^{53} \mod 77 = 09$
  - $11^{53} \mod 77 = 44$
  - $11^{53} \mod 77 = 44$
  - $14^{53} \mod 77 = 49$
- Alice sends 35 09 44 44 49

### Example

- Bob receives 35 09 44 44 49
- Bob uses Alice's public key, e = 17, n = 77, to decrypt message:
  - $35^{17} \mod 77 = 07$
  - $09^{17} \mod 77 = 04$
  - $44^{17} \mod 77 = 11$
  - $44^{17} \mod 77 = 11$
  - $49^{17} \mod 77 = 14$
- Bob translates message to letters to read HELLO
  - Alice sent it as only she knows her private key, so no one else could have enciphered it
  - If (enciphered) message's blocks (letters) altered in transit, would not decrypt properly

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### Example: Both

- Alice wants to send Bob message HELLO both enciphered and authenticated (integrity-checked)
  - Alice's keys: public (17, 77); private: 53
  - Bob's keys: public: (37, 77); private: 13
- Alice enciphers HELLO (07 04 11 11 14):
  - $(07^{53} \mod 77)^{37} \mod 77 = 07$
  - $(04^{53} \mod 77)^{37} \mod 77 = 37$
  - $(11^{53} \mod 77)^{37} \mod 77 = 44$
  - $(11^{53} \mod 77)^{37} \mod 77 = 44$
  - $(14^{53} \mod 77)^{37} \mod 77 = 14$
- Alice sends 07 37 44 44 14

## Security Services

- Confidentiality
  - Only the owner of the private key knows it, so text enciphered with public key cannot be read by anyone except the owner of the private key
- Authentication
  - Only the owner of the private key knows it, so text enciphered with private key must have been generated by the owner

## More Security Services

- Integrity
  - Enciphered letters cannot be changed undetectably without knowing private key
- Non-Repudiation
  - Message enciphered with private key came from someone who knew it

## Warnings

- Encipher message in blocks considerably larger than the examples here
  - If 1 character per block, RSA can be broken using statistical attacks (just like classical cryptosystems)
  - Attacker cannot alter letters, but can rearrange them and alter message meaning
    - Example: reverse enciphered message of text ON to get NO

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# Cryptographic Checksums

- Mathematical function to generate a set of k bits from a set of n bits (where  $k \le n$ ).
  - k is smaller then n except in unusual circumstances
- Example: ASCII parity bit
  - ASCII has 7 bits; 8th bit is "parity"
  - Even parity: even number of 1 bits
  - Odd parity: odd number of 1 bits

### Example Use

- Bob receives "10111101" as bits.
  - Sender is using even parity; 6 1 bits, so character was received correctly
    - Note: could be garbled, but 2 bits would need to have been changed to preserve parity
  - Sender is using odd parity; even number of 1
     bits, so character was not received correctly

#### Definition

- Cryptographic checksum  $h: A \rightarrow B$ :
  - 1. For any  $x \in A$ , h(x) is easy to compute
  - 2. For any  $y \in B$ , it is computationally infeasible to find  $x \in A$  such that h(x) = y
  - 3. It is computationally infeasible to find two inputs  $x, x' \in A$  such that  $x \neq x'$  and h(x) = h(x')
    - Alternate form (stronger): Given any  $x \in A$ , it is computationally infeasible to find a different  $x' \in A$ such that h(x) = h(x').

### Collisions

- If  $x \neq x'$  and h(x) = h(x'), x and x' are a *collision* 
  - Pigeonhole principle: if there are *n* containers for *n*+1 objects, then at least one container will have 2 objects in it.
  - Application: if there are 32 files and 8 possible cryptographic checksum values, at least one value corresponds to at least 4 files

## Keys

- Keyed cryptographic checksum: requires cryptographic key
  - DES in chaining mode: encipher message, use last *n* bits. Requires a key to encipher, so it is a keyed cryptographic checksum.
- Keyless cryptographic checksum: requires no cryptographic key
  - MD5 and SHA-1 are best known; others include MD4, HAVAL, and Snefru

### HMAC

- Make keyed cryptographic checksums from keyless cryptographic checksums
- *h* keyless cryptographic checksum function that takes data in blocks of *b* bytes and outputs blocks of *l* bytes. *k'* is cryptographic key of length *b* bytes

– If short, pad with 0 bytes; if long, hash to length *b* 

- *ipad* is 00110110 repeated b times
- *opad* is 01011100 repeated *b* times
- HMAC- $h(k, m) = h(k' \oplus opad \parallel h(k' \oplus ipad \parallel m))$ 
  - $\oplus$  exclusive or, || concatenation

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# Key Points

- Two main types of cryptosystems: classical and public key
- Classical cryptosystems encipher and decipher using the same key
  - Or one key is easily derived from the other
- Public key cryptosystems encipher and decipher using different keys
  - Computationally infeasible to derive one from the other
- Cryptographic checksums provide a check on integrity

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