

## Outline for May 27, 2009

Reading: §13.2

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1. Recursion
  - a. Express problem in terms of itself
  - b. Recursive definitions
    - i. Base case (not recursive)
    - ii. Recursive part (must eventually reduce to base case)
  - c. Relationship to mathematical induction
2. Example:  $n!$  (see fact.py)
  - a. Definition
    - i. Base case:  $0! = 1$
    - ii. Recursive part:  $n! = n(n-1)!$
  - b. Show stack for  $n = 3$
3. Example: reverse string (see reverse.py)
  - a. Definition
    - i. Base case: empty string
    - ii. Recursive part:  $\text{reverse}(s) = \text{reverse}(s[1:]) + s[0]$
  - b. Show stack for  $\text{str} = \text{"yes"}$
4. Example: binary search (see binsearch.py)
  - a. Definition
    - i. Base case:  $\text{high} < \text{low}$ , return failure; word is  $\text{list}[\text{mid}]$ , return  $\text{mid}$
    - ii. Recursive part: if  $\text{word} < \text{list}[\text{mid}]$ , search  $\text{word}[0..\text{mid}-1]$ ; if  $\text{word} > \text{list}[\text{mid}]$ , search  $\text{word}[\text{mid}+1..\text{high}]$
  - b. Show for list.txt from last time
5. Example: list of permutations of string (see perm.py)
  - a. Definition
    - i. Base case: empty string gives list of empty string
    - ii. Recursive part: for each permutation of (string without first char), put first letter of this string in each position
  - b. Show stack for  $s = \text{"012"}$
6. Example: Fibonacci numbers (see rfib.py)
  - a. Definition
    - i. Base case:  $\text{fib}(0) = 1$ ,  $\text{fib}(1) = 1$
    - ii. Recursive part:  $\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$
  - b. Show stack for  $n = 3$