

# Cipher Techniques

ECS 153 Spring Quarter 2021

Module 16

# Problems

- Using cipher requires knowledge of environment, and threats in the environment, in which cipher will be used
  - Is the set of possible messages small?
  - Can an active wiretapper rearrange or change parts of the message?
  - Do the messages exhibit regularities that remain after encipherment?
  - Can the components of the message be misinterpreted?

# Attack #1: Precomputation

- Set of possible messages  $M$  small
- Public key cipher  $f$  used
- Idea: precompute set of possible ciphertexts  $f(M)$ , build table  $(m, f(m))$
- When ciphertext  $f(m)$  appears, use table to find  $m$
- Also called *forward searches*

# Example

- Cathy knows Alice will send Bob one of two messages: enciphered BUY, or enciphered SELL
- Using public key  $e_{Bob}$ , Cathy precomputes
$$m_1 = \{ \text{BUY} \} e_{Bob}, m_2 = \{ \text{SELL} \} e_{Bob}$$
- Cathy sees Alice send Bob  $m_2$
- Cathy knows Alice sent SELL

# May Not Be Obvious

- Digitized sound
  - Seems like far too many possible plaintexts, as initial calculations suggest  $2^{32}$  such plaintexts
  - Analysis of redundancy in human speech reduced this to about 100,000 ( $\approx 2^{17}$ ), small enough for precomputation attacks

# Misordered Blocks

- Alice sends Bob message
  - $n_{Bob} = 262631, e_{Bob} = 45539, d_{Bob} = 235457$
- Message is TOMNOTANN (191412 131419 001313)
- Enciphered message is 193459 029062 081227
- Eve intercepts it, rearranges blocks
  - Now enciphered message is 081227 029062 193459
- Bob gets enciphered message, deciphers it
  - He sees ANNNOTTOM, opposite of what Alice sent

# Solution

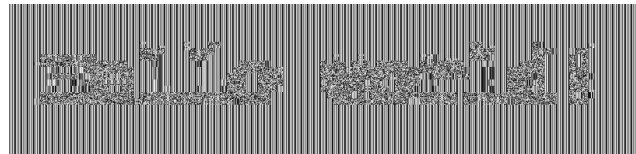
- Digitally signing each block won't stop this attack
- Two approaches:
  - Cryptographically hash the *entire* message and sign it
  - Place sequence numbers in each block of message, so recipient can tell intended order; then sign each block

# Statistical Regularities

- If plaintext repeats, ciphertext may too
- Example using AES-128:

- Input image: `Hello world!`

- corresponding output image:

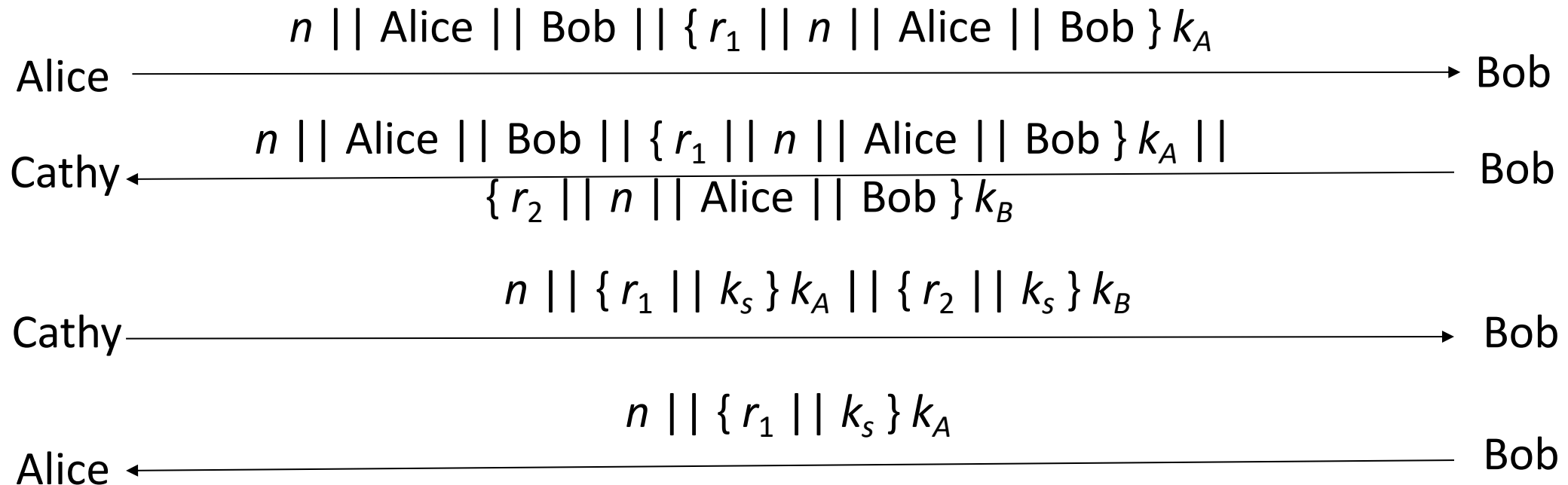


- Note you can still make out the words
  - Fix: cascade blocks together (chaining) More details later



# Type Flaw Attacks

- Assume components of messages in protocol have particular meaning
- Example: Otway-Rees:



# The Attack

- Ichabod intercepts message from Bob to Cathy in step 2
- Ichabod *replays* this message, sending it to Bob
  - Slight modification: he deletes the cleartext names
- Bob *expects*  $n \parallel \{ r_1 \parallel k_s \} k_A \parallel \{ r_2 \parallel k_s \} k_B$
- Bob *gets*  $n \parallel \{ r_1 \parallel n \parallel \text{Alice} \parallel \text{Bob} \} k_A \parallel \{ r_2 \parallel n \parallel \text{Alice} \parallel \text{Bob} \} k_B$
- So Bob sees  $n \parallel \text{Alice} \parallel \text{Bob}$  as the session key — and Ichabod knows this
- When Alice gets her part, she makes the same assumption
- Now Ichabod can read their encrypted traffic

# Solution

- Tag components of cryptographic messages with information about what the component is
  - But the tags themselves may be confused with data ...

# What These Mean

- Use of strong cryptosystems, well-chosen (or random) keys not enough to be secure
- Other factors:
  - Protocols directing use of cryptosystems
  - Ancillary information added by protocols
  - Implementation (not discussed here)
  - Maintenance and operation (not discussed here)

# Stream, Block Ciphers

- $E$  encipherment function
  - $E_k(b)$  encipherment of message  $b$  with key  $k$
  - In what follows,  $m = b_1b_2 \dots$ , each  $b_i$  of fixed length
- Block cipher
  - $E_k(m) = E_k(b_1)E_k(b_2) \dots$
- Stream cipher
  - $k = k_1k_2 \dots$
  - $E_k(m) = E_{k_1}(b_1)E_{k_2}(b_2) \dots$
  - If  $k_1k_2 \dots$  repeats itself, cipher is *periodic* and the length of its period is one cycle of  $k_1k_2 \dots$

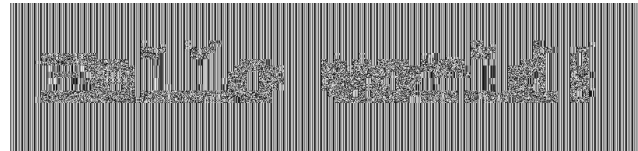
# Example

- AES-128
  - $b_i = 128$  bits,  $k = 128$  bits
  - Each  $b_i$  enciphered separately using  $k$
  - Block cipher

# Block Ciphers

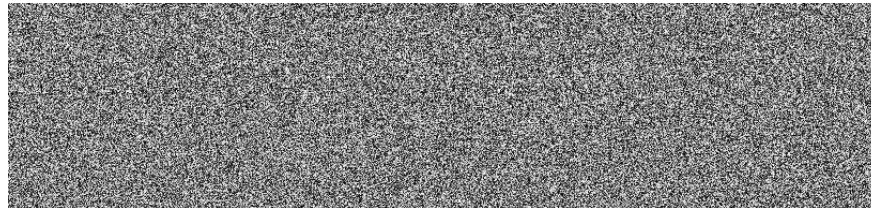
- Encipher, decipher multiple bits at once
- Each block enciphered independently
- Problem: identical plaintext blocks produce identical ciphertext blocks
- Plaintext image: `Hello world!`

- Ciphertext image:



# Solutions

- Insert information about block's position into the plaintext block, then encipher
- *Cipher block chaining*:
  - Exclusive-or current plaintext block with previous ciphertext block:
    - $c_0 = E_k(m_0 \oplus I)$
    - $c_i = E_k(m_i \oplus c_{i-1})$  for  $i > 0$
  - where  $I$  is the initialization vector
- Example encipherment of image on previous slide:





# Authenticated Encryption

- Transforms message providing confidentiality, integrity, authentication simultaneously
- May be associated data that is not to be encrypted
  - Called Authenticated Encryption with Associated Data (AEAD)
- An examples:
  - Galois Counter Mode (GCM)
- *message* is part to be encrypted; *associated data* is part not to be encrypted
  - Both are authenticated and integrity-checked; if omitted, treat as having length 0

# Galois Counter Mode (GCM)

- Can be implemented efficiently in hardware
- If encrypted, authenticated message is changed, new authentication value can be computed with cost proportional to number of changed bits
- Allows nonce (initialization vector) of any length
- Parameters
  - nonce  $IV$  up to  $2^{64}$  bits; 96 bits recommended for efficiency reasons
  - message  $M$  up to  $2^{39} - 2^8$  bits long; ciphertext  $C$  same length
  - associated data  $A$  up to  $2^{64}$  bits long

# GCM Notation

- Authentication value  $T$  is  $t$  bits long
- $M = M_0 \dots M_n$ , each block 128 bits long
  - $M_n$  may not be complete block; call its length  $u$  bits
- $C = C_0 \dots C_n$ , each block 128 bits long;  $C$  is  $L_C$  bits long
  - Number of bits in  $C$  is the same as number of bits in  $M$
- $A = A_0 \dots A_m$ , each block 128 bits long;  $A$  is  $L_A$  bits long
  - $A_m$  may not be complete block; call its length  $v$  bits
- $0^x, 1^y$  mean  $x$  bits of 0 and  $y$  bits of 1, respectively

# Multiplication in $GF(2^{128})$

```
/* multiply X and Y to produce Z in GF (2^128 ) */
```

```
function GFmultiply(X, Y: integer )
```

```
begin
```

```
    Z := 0
```

```
    V := X;
```

```
    for i := 0 to 127 do begin
```

```
        if  $Y_i = 1$  then Z :=  $Z \oplus V$ ;
```

```
        V = rightshift(V, 1);
```

```
        if  $V_{127} = 1$  then V :=  $V \oplus R$ ;
```

```
    end
```

```
    return Z;
```

```
end
```

- This is written  $Z = X \cdot Y$
- $Y_i$  is  $i$ th leftmost bit of  $Y$ , so  $Y_{127}$  is the rightmost bit of  $Y$
- rightshift( $V$ , 1) means to shift  $V$  right 1 bit, and bring in 0 from the left
- $R$  is bits 11100001 followed by 120 0 bits

# GCM Hash Function

GHASH( $H, A, C$ ) computed as follows:

1.  $X_0 = 0$
2. for  $i = 1, \dots, m-1$ ,  $X_i = (X_{i-1} \oplus A_i) \cdot H$
3.  $X_m = (X_{m-1} \oplus A_m) \cdot H$ 
  - $A_m$  is right-padded with 0s if not a complete block
4. for  $i = m+1, \dots, m+n-1$ ,  $X_i = (X_{i-1} \oplus C_i) \cdot H$
5.  $X_{m+n} = (X_{m+n-1} \oplus C_n) \cdot H$ 
  - $C_n$  is right-padded with 0s if not a complete block
6.  $X_{m+n+1} = (X_{m+n} \oplus (L_A || L_C)) \cdot H$ 
  - $L_A, L_C$  left-padded with 0 bits to form 64 bits each

# GCM Authenticated Encryption

This computes  $C$  and  $T$ :

1.  $H = E_k(0^{128})$
2. If  $IV$  is 96 bits,  $Y_0 = IV \parallel 0^{31}1$ ; otherwise,  $Y_0 = \text{GHASH}(H, \nu, IV)$ 
  - $\nu$  empty string
3. for  $i = 1, \dots, n$ ,  $l_i = l_{i-1} + 1 \bmod 2^{32}$ ; set  $Y_i = L_{i-1} \parallel l_i$ 
  - $l_{i-1}$  right part of  $Y_{i-1}$ ; treat it as unsigned 32 bit integer;  $L_{i-1}$  left part of  $Y_{i-1}$
4. for  $i = 1, \dots, n-1$ ,  $C_i = M_i + E_k(Y_i)$
5.  $C_n = M_n + \text{MSB}_u(E_k(Y_n))$ 
  - $\text{MSB}_u(X)$  is  $u$  most significant (leftmost) bits of  $X$
6.  $T = \text{MSB}_t(\text{GHASH}(H, A, C) + E_k(Y_0))$

# GCM Transmission and Decryption

- Send  $C, T$
- To verify, perform steps 1, 2, 6, 3, 4, 5
- When authentication value is computed, compare to sent value
  - Note this is done *before* decrypting the message
  - If they do not match, return failure and discard messages

# GCM Analysis

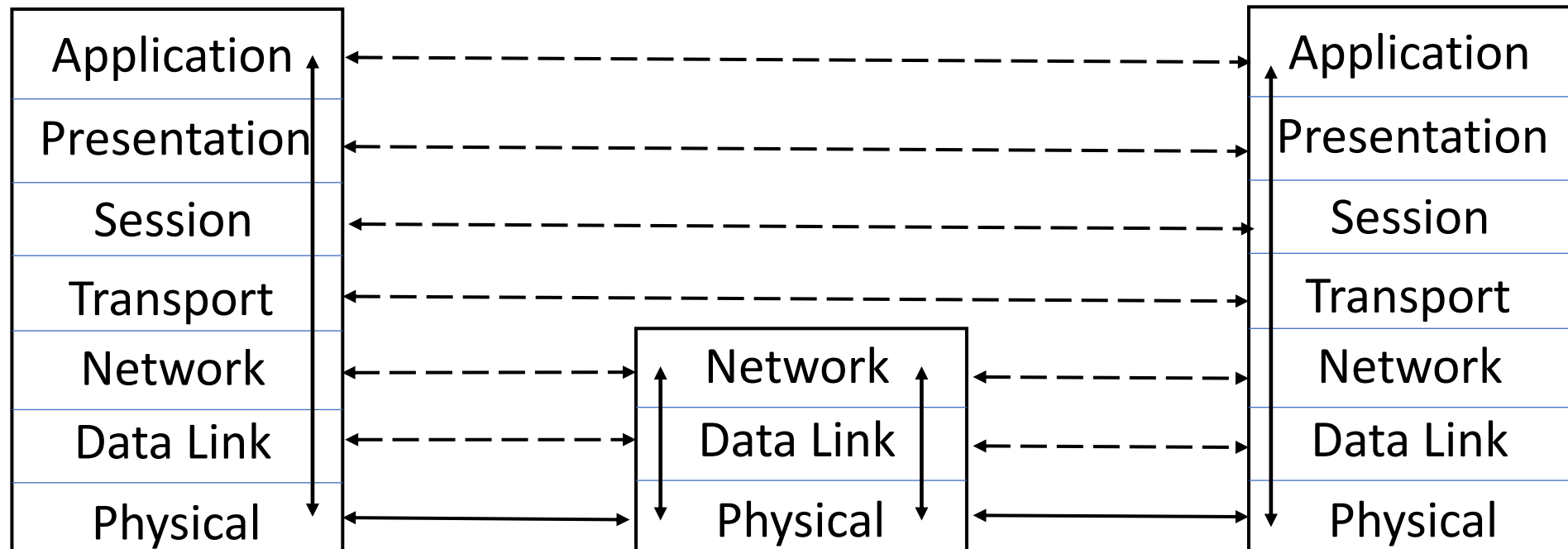
Strength depends on certain properties

- If  $IV$  (nonce) reused, part of  $H$  can be obtained
- If length of authentication value too short, forgeries can occur and from that,  $H$  can be determined (enabling undetectable forgeries)
- Under study is whether particular values of  $H$  make forging messages easier
- Restricting length of  $IV$  to 96 bits produces a stronger AEAD cipher than when the length is not restricted



# Networks and Cryptography

- ISO/OSI model
- Conceptually, each host communicates with peer at each layer

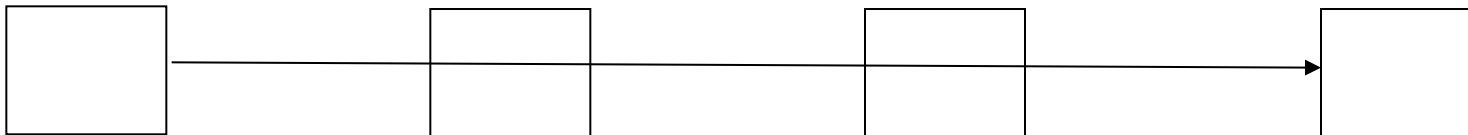


# Link and End-to-End Protocols

## Link Protocol



## End-to-End (or E2E) Protocol



# Encryption

- Link encryption
  - Each host enciphers message so host at “next hop” can read it
  - Message can be read at intermediate hosts
- End-to-end encryption
  - Host enciphers message so host at other end of communication can read it
  - Message cannot be read at intermediate hosts

# Examples

- SSH protocol
  - Messages between client, server are enciphered, and encipherment, decipherment occur only at these hosts
  - End-to-end protocol
- PPP Encryption Control Protocol
  - Host gets message, decipheres it
    - Figures out where to forward it
    - Enciphers it in appropriate key and forwards it
  - Link protocol

# Cryptographic Considerations

- Link encryption
  - Each host shares key with neighbor
  - Can be set on per-host or per-host-pair basis
    - Windsor, stripe, seaview each have own keys
    - One key for (windsor, stripe); one for (stripe, seaview); one for (windsor, seaview)
- End-to-end
  - Each host shares key with destination
  - Can be set on per-host or per-host-pair basis
  - Message cannot be read at intermediate nodes

# Traffic Analysis

- Link encryption
  - Can protect headers of packets
  - Possible to hide source and destination
    - Note: may be able to deduce this from traffic flows
- End-to-end encryption
  - Cannot hide packet headers
    - Intermediate nodes need to route packet
  - Attacker can read source, destination

# Example Protocols

- Securing Electronic Mail (OpenPGP, PEM)
  - Applications layer protocol
  - Start with PEM as goals, design described in detail; then look at OpenPGP
- Securing Instant Messaging (Signal)
  - Applications layer protocol
- Secure Socket Layer (TLS)
  - Transport layer protocol
- IP Security (IPSec)
  - Network layer protocol

# Transport Layer Security

- Internet protocol: TLS
  - Provides confidentiality, integrity, authentication of endpoints
  - Focus on version 1.2
- Old Internet protocol: SSL
  - Developed by Netscape for WWW browsers and servers
  - Use is deprecated



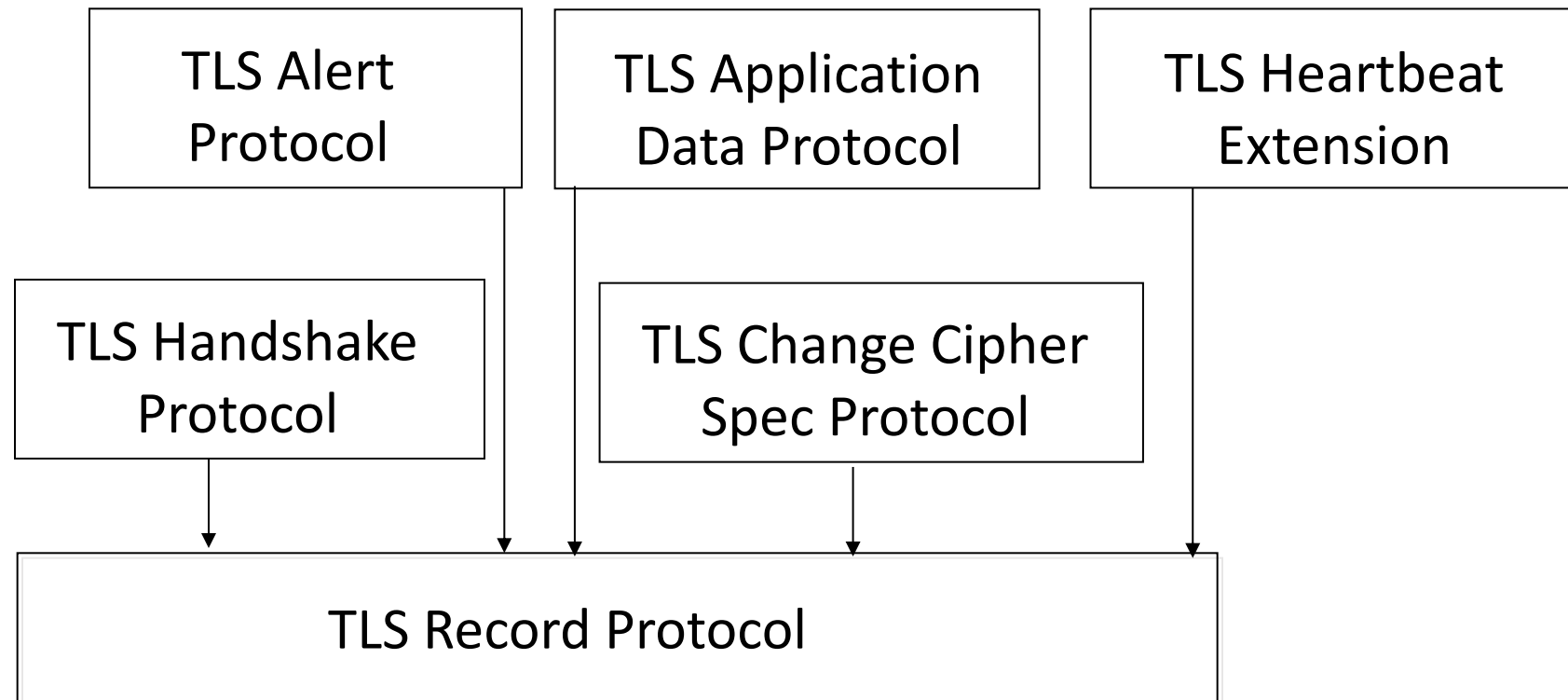
# TLS Session

- Association between two peers
  - May have many associated connections
  - Information related to session for each peer:
    - Unique session identifier
    - Peer's X.509v3 certificate, if needed
    - Compression method
    - Cipher spec for cipher and MAC
    - "Master secret" of 48 bits shared with peer
    - Flag indicating whether this session can be used to start new connection

# TLS Connection

- Describes how data exchanged with peer
- Information for each connection
  - Whether a server or client
  - Random data for server and client
  - Write keys (used to encipher data)
  - Write MAC key (used to compute MAC)
  - Initialization vectors for ciphers, if needed
  - Sequence numbers for server, client

# Structure of TLS



# Supporting Cryptography

- All parts of TLS use them
- Initial phase: public key system exchanges keys
  - Messages enciphered using classical ciphers, checksummed using cryptographic checksums
  - Only certain combinations allowed
    - Depends on algorithm for interchange cipher
  - Interchange algorithms: RSA, Diffie-Hellman

# Diffie-Hellman: Types

- Diffie-Hellman: certificate contains D-H parameters, signed by a CA
  - DSS or RSA algorithms used to sign
- Ephemeral Diffie-Hellman: DSS or RSA certificate used to sign D-H parameters
  - Parameters not reused, so not in certificate
- Anonymous Diffie-Hellman: D-H with neither party authenticated
  - Use is “strongly discouraged” as it is vulnerable to attacks
- Elliptic curve Diffie-Hellman supports Diffie-Hellman and ephemeral Diffie-Hellman
  - But not anonymous Diffie-Hellman

# Derivation of Master Secret

- $master\_secret = PRF(premaster, \text{"master secret"}, r_1 || r_2)$ 
  - $premaster$  set by client, ° sent to server during setup
  - $r_1, r_2$  random numbers from client, server respectively
- $PRF(secret, label, seed) = P\_hash(secret, label || seed)$
- $P\_hash(secret, seed) = \text{HMAC\_hash}(secret || A(1) || seed) ||$   
 $\text{HMAC\_hash}(secret || A(2) || seed) ||$   
 $\text{HMAC\_hash}(secret || A(3) || seed) || \dots$ 
  - Use first 48 bits of output to set  $PRF$
- $A(0) = seed, A(i) = \text{HMAC\_hash}(secret, A(i-1))$  for  $i > 0$

# Derivation of Keys

- $key\_block = \text{PRF}(master, \text{“key expansion”}, r_1 || r_2)$ 
  - $r_1, r_2$  as before
- Break it into blocks of 48 bits
  - First two are client, server keys for computing MACs
  - Next two are client, server keys used to encipher messages
  - Next two are client, server initialization vectors
    - Omitted if cipher does not use initialization vector

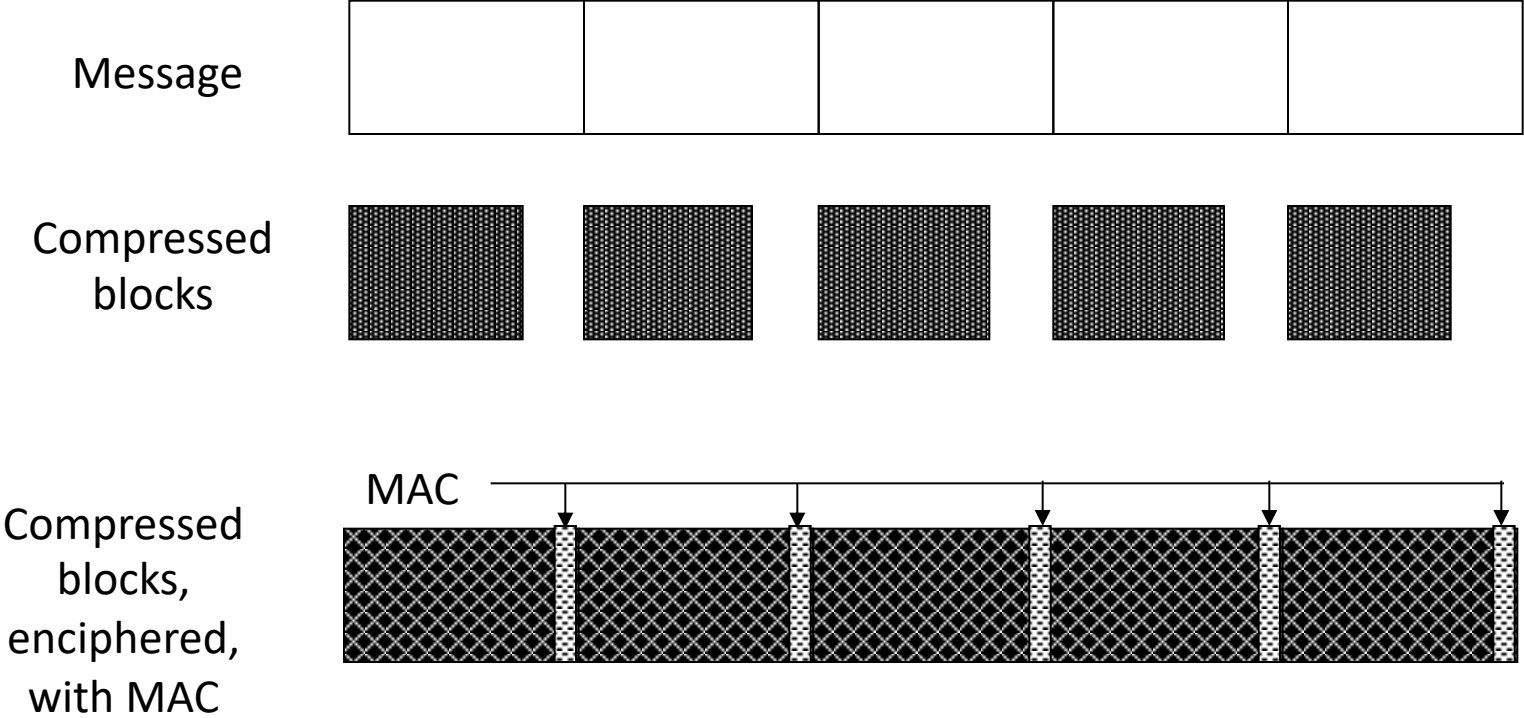
# MAC for Block

*hash(MAC\_ws, seq || TLS\_comp || TLS\_vers || TLS\_len || block)*

- *MAC\_ws*: MAC write key
- *seq*: sequence number of *block*
- *TLS\_comp*: message type
- *TLS\_vers*: TLS version
- *TLS\_len*: length of *block*
- *block*: block being sent



# TLS Record Layer



# Record Protocol Overview

- Lowest layer, taking messages from higher
  - Max block size  $2^{14} = 16,384$  bytes
  - Bigger messages split into multiple blocks
- Construction
  - Block  $b$  compressed; call it  $b_c$
  - MAC computed for  $b_c$ 
    - If MAC key not selected, no MAC computed
  - $b_c$ , MAC enciphered
    - If enciphering key not selected, no enciphering done
  - TLS record header prepended

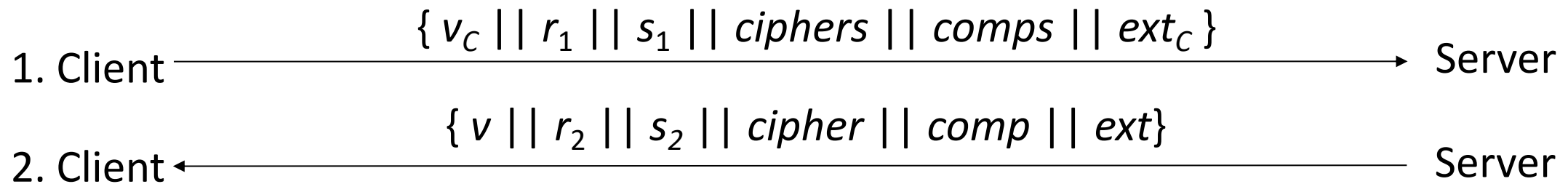
# TLS Handshake Protocol

- Used to initiate connection
  - Sets up parameters for record protocol
  - 4 rounds
- Upper layer protocol
  - Invokes Record Protocol
- Note: what follows assumes client, server using RSA as interchange cryptosystem

# Overview of Rounds

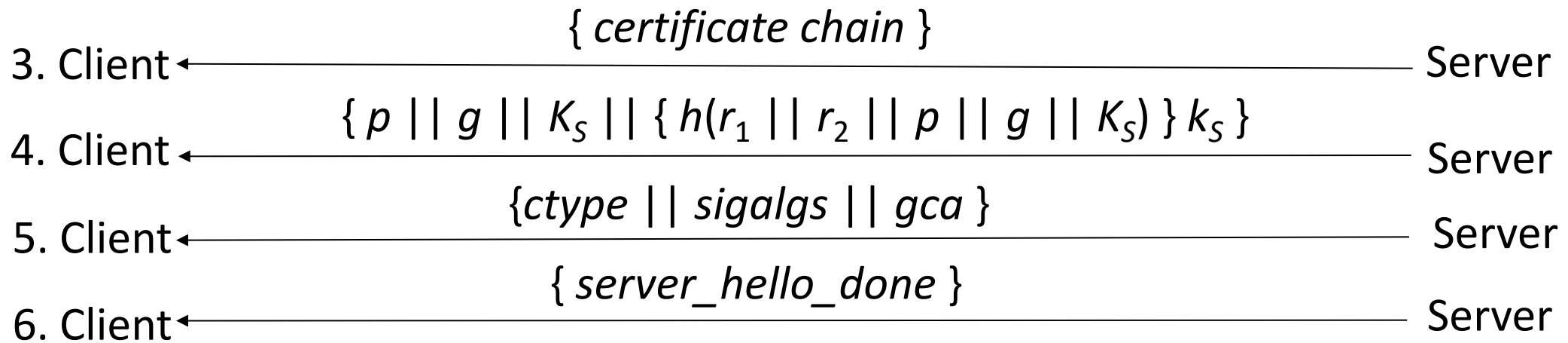
1. Create TLS connection between client, server
2. Server authenticates itself
3. Client validates server, begins key exchange
4. Acknowledgments all around

# Handshake Round 1



- $v_C$  Client's version of TLS
- $v$  Highest version of TLS that client, server both understand
- $r_1, r_2$  nonces (timestamp and 28 random bytes)
- $s_1$  Current session id (empty if new session)
- $s_2$  Current session id (if  $s_1$  empty, new session id)
- $ciphers$  Ciphers that client understands
- $comps$  Compression algorithms that client understand
- $cipher$  Cipher to be used
- $comp$  Compression algorithm to be used
- $ext_C$  List of extensions client supports
- $ext$  List of extensions server supports (subset of  $ext_C$ )

# Handshake Round 2



If server not going to authenticate itself, only last message sent

Second step is for Diffie-Hellman with RSA certificate

Third step omitted if server does not need client certificate

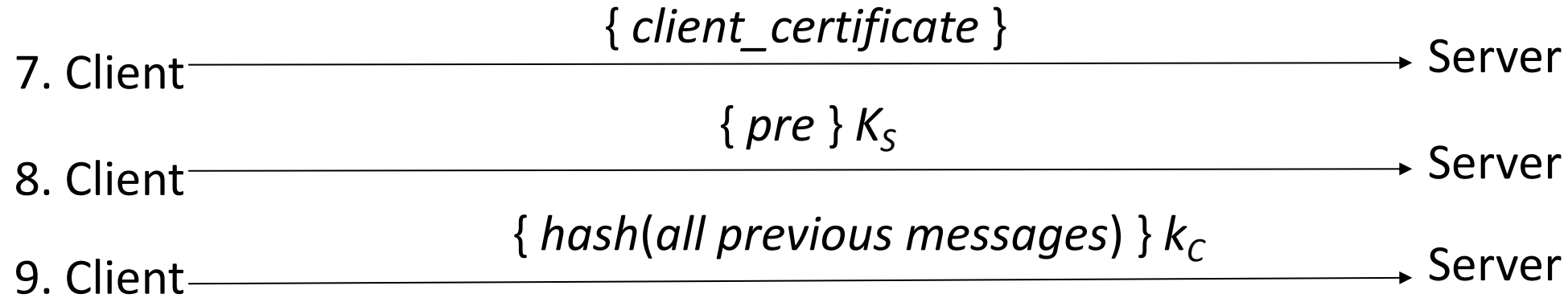
$K_S, k_S$  Server's Diffie-Hellman public, private keys

$\textit{ctype}$  Certificate type accepted (by cryptosystem)

$\textit{sigalgs}$  List of hash, signature algorithm pairs server can use

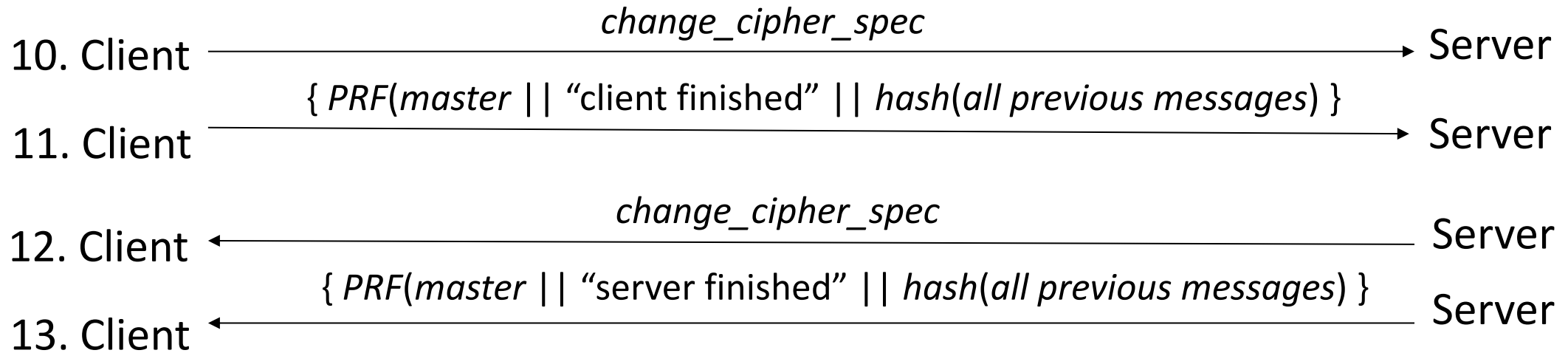
$\textit{gca}$  Acceptable certification authorities

# Handshake Round 3



$pre$	Premaster secret
$K_S$	Server's public key
$k_C$	Client's private key

# Handshake Round 4



*change\_cipher\_spec*

Begin using cipher specified



# TLS Change Cipher Spec Protocol

- Send single byte
- In handshake, new parameters considered “pending” until this byte received
  - Old parameters in use, so cannot just switch to new ones

# TLS Alert Protocol

- Closure alert
  - Sender will send no more messages
  - Pending data delivered; new messages ignored
- Error alerts
  - Warning: connection remains open
  - Fatal error: connection torn down as soon as sent or received

# TLS Heartbeat Extension

- Message has 4 fields
  - Value indicating message is request
  - Length of data in message
  - Data of given length
  - Random data
- Message sent to peer; peer replies with similar message
  - If second field is too large ( $> 2^{14}$  bytes), ignore message
  - Reply message has same data peer sent, new random data
- When peer sends this for the first time, it sends nothing more until a response is received

# TLS Application Data Protocol

- Passes data from application to TLS Record Protocol layer

# Differences Between TLSv2 and SSLv3

- SSLv3 master secret computed differently

$$\begin{aligned} \text{master} = & \text{MD5}(\text{premaster} \parallel \text{SHA}(\text{'A'} \parallel \text{premaster} \parallel r_1 \parallel r_2) \parallel \\ & \text{MD5}(\text{premaster} \parallel \text{SHA}(\text{'BB'} \parallel \text{premaster} \parallel r_1 \parallel r_2) \parallel \\ & \text{MD5}(\text{premaster} \parallel \text{SHA}(\text{'CCC'} \parallel \text{premaster} \parallel r_1 \parallel r_2) \end{aligned}$$

- SSLv3 key block also computed differently

$$\begin{aligned} \text{key\_block} = & \text{MD5}(\text{master} \parallel \text{SHA}(\text{'A'} \parallel \text{master} \parallel r_1 \parallel r_2) \parallel \\ & \text{MD5}(\text{master} \parallel \text{SHA}(\text{'BB'} \parallel \text{master} \parallel r_1 \parallel r_2) \parallel \\ & \text{MD5}(\text{master} \parallel \text{SHA}(\text{'CCC'} \parallel \text{master} \parallel r_1 \parallel r_2) \parallel \dots \end{aligned}$$

# Differences Between TLSv2 and SSLv3

SSLv3 MAC for each block computed differently:

$hash(MAC\_ws \parallel opad \parallel$

$hash(MAC\_ws \parallel ipad \parallel seq \parallel SSL\_comp \parallel SSL\_len \parallel block))$

- *hash*: hash function used
- *MAC\_ws, seq, SSL\_comp, SSL\_len, block*: as for TLS (with obvious changes)
- *ipad, opad*: as for HMAC

# Differences Between TLSv2 and SSLv3

- Verification message (9, above) is different:

9'. Client  $\xrightarrow{\{ \textit{hash}(\textit{master} || \textit{opad} || \textit{hash}(\textit{all previous messages} || \textit{master} || \textit{ipad})) \}}$  Server

- Messages after change cipher spec (11, 13 above) are also different:

11'. Client  $\xrightarrow{\{ \textit{hash}(\textit{master} || \textit{opad} || \textit{hash}(\textit{all previous messages} || 0x434C4E54 || \textit{master} || \textit{ipad})) \}}$  Server

13'. Client  $\xrightarrow{\{ \textit{hash}(\textit{master} || \textit{opad} || \textit{hash}(\textit{all previous messages} || 0x53525652 || \textit{master} || \textit{ipad})) \}}$  Server

# Differences Between TLSv2 and SSLv3

- Different sets of ciphers
  - SSL allows use of RC4, but its use is deprecated
  - SSL allows set of ciphers for the Fortezza cryptographic token used by the U.S. Department of Defense



# Problems with SSL

- POODLE attack focuses on padding of messages
  - In SSL, all but the last byte of the padding are random and so cannot be checked
- How padding works (assume block size of  $b$ ):
  - Message ends in a full block: add additional block of padding, and last byte is the number of bytes of random padding ( $b - 1$ )
  - Message ends in part of a block: add random bytes out to last byte, set that to number of random bytes (so if block is  $b - 1$  bytes, one padding byte added and it is 0)

# The POODLE Attack

- Peer receives incoming ciphertext message  $c_1, \dots, c_n$
- Peer decrypts it to  $m_1, \dots, m_n$ :  $m_i = D_k(c_i) \oplus c_{i-1}$ , where  $c_0$  is initialization vector
  - Validates by removing padding, computes and checks MAC over remaining bytes
- Attacker replaces  $c_n$  with some earlier block, say  $c_j, j \neq n$ 
  - If last byte of  $c_j$  is same as  $c_n$ , message accepted as valid; otherwise, rejected
- So attacker arranges for HTTP messages to end with known number of padding bytes
  - Then server should accept changed message in at least 1 out of 256 tries

# Example POODLE Attack

- Here's HTTP request (somewhat simplified):

GET / HTTP/1.1\r\n Cookie: abcdefgh \r\n\r\nxxxxx MAC ●●●●●●7

- Attacker cannot see plaintext
- Run Javascript in browser that duplicates cookie block and overwrites last block
  - It's enciphered using (for example) 3DES-CBC
- You see enciphered block
  - If it is accepted, then plaintext block xor'ed with previous ciphertext block ends in 7

# SSL, TLS, and POODLE

- POODLE serious enough that SSL is being discarded in favor of TLS
- TLS not vulnerable, as all padding bytes set to length of padding
  - And TLS implementations must check this padding (all of it) for validity before accepting messages