

# April 5: ACM and Safety

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- Protection State Transitions
  - Commands
  - Conditional Commands
- Special Rights
  - Principle of Attenuation of Privilege
- Harrison-Ruzzo-Ullman result
  - Corollaries

# State Transitions

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- Change the protection state of system
- $\vdash$  represents transition
  - $X_i \vdash_{\tau} X_{i+1}$ : command  $\tau$  moves system from state  $X_i$  to  $X_{i+1}$
  - $X_i \vdash^* Y$ : a sequence of commands moves system from state  $X_i$  to  $Y$
- Commands often called *transformation procedures*

# Primitive Operations

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- **create subject  $s$ ; create object  $o$** 
  - Creates new row, column in ACM; creates new column in ACM
- **destroy subject  $s$ ; destroy object  $o$** 
  - Deletes row, column from ACM; deletes column from ACM
- **enter  $r$  into  $A[s, o]$** 
  - Adds  $r$  rights for subject  $s$  over object  $o$
- **delete  $r$  from  $A[s, o]$** 
  - Removes  $r$  rights from subject  $s$  over object  $o$

# Create Subject

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- Precondition:  $s \notin S$
- Primitive command: **create subject  $s$**
- Postconditions:
  - $S' = S \cup \{ s \}, O' = O \cup \{ s \}$
  - $(\forall y \in O') [a'[s, y] = \emptyset], (\forall x \in S') [a'[x, s] = \emptyset]$
  - $(\forall x \in S)(\forall y \in O) [a'[x, y] = a[x, y]]$

# Create Object

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- Precondition:  $o \notin O$
- Primitive command: **create object  $o$**
- Postconditions:
  - $S' = S, O' = O \cup \{ o \}$
  - $(\forall x \in S') [a'[x, o] = \emptyset]$
  - $(\forall x \in S)(\forall y \in O) [a'[x, y] = a[x, y]]$

# Add Right

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- Precondition:  $s \in S, o \in O$
- Primitive command: enter  $r$  into  $a[s, o]$
- Postconditions:
  - $S' = S, O' = O$
  - $a'[s, o] = a[s, o] \cup \{ r \}$
  - $(\forall x \in S')(\forall y \in O' - \{ o \}) [a'[x, y] = a[x, y]]$
  - $(\forall x \in S' - \{ s \})(\forall y \in O') [a'[x, y] = a[x, y]]$

# Delete Right

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- Precondition:  $s \in S, o \in O$
- Primitive command: **delete  $r$  from  $a[s, o]$**
- Postconditions:
  - $S' = S, O' = O$
  - $a'[s, o] = a[s, o] - \{ r \}$
  - $(\forall x \in S')(\forall y \in O' - \{ o \}) [a'[x, y] = a[x, y]]$
  - $(\forall x \in S' - \{ s \})(\forall y \in O') [a'[x, y] = a[x, y]]$

# Destroy Subject

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- Precondition:  $s \in S$
- Primitive command: **destroy subject  $s$**
- Postconditions:
  - $S' = S - \{ s \}, O' = O - \{ s \}$
  - $(\forall y \in O') [a'[s, y] = \emptyset], (\forall x \in S') [a'[x, s] = \emptyset]$
  - $(\forall x \in S')(\forall y \in O') [a'[x, y] = a[x, y]]$



# Destroy Object

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- Precondition:  $o \in O$
- Primitive command: **destroy object  $o$**
- Postconditions:
  - $S' = S, O' = O - \{ o \}$
  - $(\forall x \in S') [a'[x, o] = \emptyset]$
  - $(\forall x \in S')(\forall y \in O') [a'[x, y] = a[x, y]]$

# Creating File

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- Process  $p$  creates file  $f$  with  $r$  and  $w$  permission

```
command create•file( $p$ ,  $f$ )  
    create object  $f$ ;  
    enter own into  $A[p, f]$ ;  
    enter  $r$  into  $A[p, f]$ ;  
    enter  $w$  into  $A[p, f]$ ;  
end
```

# Mono-Operational Commands

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- Make process  $p$  the owner of file  $g$   
**command** *make-owner*( $p, g$ )  
    **enter own into**  $A[p, g]$ ;  
**end**
- Mono-operational command
  - Single primitive operation in this command

# Conditional Commands

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- Let  $p$  give  $q$   $r$  rights over  $f$ , if  $p$  owns  $f$   
**command**  $grant \cdot read \cdot file \cdot 1(p, f, q)$   
    **if**  $own$  **in**  $A[p, f]$   
    **then**  
        **enter**  $r$  **into**  $A[q, f];$   
    **end**
- Mono-conditional command
  - Single condition in this command

# Multiple Conditions

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- Let  $p$  give  $q$   $r$  and  $w$  rights over  $f$ , if  $p$  owns  $f$  and  $p$  has  $c$  rights over  $q$

```
command grant•read•file•2( $p, f, q$ )  
    if own in  $A[p, f]$  and c in  $A[p, q]$   
    then  
        enter  $r$  into  $A[q, f]$ ;  
        enter  $w$  into  $A[q, f]$ ;  
end
```

# Copy Right

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- Allows possessor to give rights to another
- Often attached to a right, so only applies to that right
  - $r$  is read right that cannot be copied
  - $rc$  is read right that can be copied
- Is copy flag copied when giving  $r$  rights?
  - Depends on model, instantiation of model

# Own Right

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- Usually allows possessor to change entries in ACM column
  - So owner of object can add, delete rights for others
  - May depend on what system allows
    - Can't give rights to specific (set of) users
    - Can't pass copy flag to specific (set of) users

# Attenuation of Privilege

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- Principle says you can't give rights you do not possess
  - Restricts addition of rights within a system
  - Usually *ignored* for owner
    - Why? Owner gives herself rights, gives them to others, deletes her rights.



# Key Points

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- Access control matrix simplest abstraction mechanism for representing protection state
- Transitions alter protection state
- 6 primitive operations alter matrix
  - Transitions can be expressed as commands composed of these operations and, possibly, conditions

# Foundational Results

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- Overview
- Harrison-Ruzzo-Ullman result
  - Corollaries
- Take-Grant Protection Model
- SPM and successors
- Expressiveness and comparing model properties

# Overview

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- Safety Question
- HRU Model
- Take-Grant Protection Model
- SPM, ESPM
  - Multiparent joint creation
- Expressive power
- Typed Access Matrix Model
- Comparing properties of models

# What Is “Secure”?

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- Adding a generic right  $r$  where there was not one is “leaking”
  - In what follows, a right leaks if it was not present *initially*
  - Alternately: not present *in the previous state*
- If a system  $S$ , beginning in initial state  $s_0$ , cannot leak right  $r$ , it is *safe with respect to the right  $r$* .

# Safety Question

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- Is there an algorithm for determining whether a protection system  $S$  with initial state  $s_0$  is safe with respect to a generic right  $r$ ?
  - Here, “safe” = “secure” for an abstract model

# Mono-Operational Commands

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- Answer: *yes*
- Sketch of proof:
  - Consider minimal sequence of commands  $c_1, \dots, c_k$  to leak the right.
    - Can omit **delete**, **destroy**
    - Can merge all **creates** into one
  - Worst case: insert every right into every entry; with  $s$  subjects and  $o$  objects initially, and  $n$  rights, upper bound is  $k \leq n(s+1)(o+1)$