

Homework #5

Due: March 15, 2024

Points: 100

Questions

1. (30 points) Let $L = (S_L, \leq_L)$ be a lattice. Define:

- (a) $S_{IL} = \{[a, b] \mid a, b \in S_L \wedge a \leq_L b\}$
- (b) $\leq_{IL} = \{([a_1, b_1], [a_2, b_2]) \mid a_1 \leq_L a_2 \wedge b_1 \leq_L b_2\}$
- (c) $\text{lub}_{IL}([a_1, b_1], [a_2, b_2]) = (\text{lub}_L(a_1, a_2), \text{lub}_L(b_1, b_2))$
- (d) $\text{glb}_{IL}([a_1, b_1], [a_2, b_2]) = (\text{glb}_L(a_1, a_2), \text{glb}_L(b_1, b_2))$

Prove that the structure $IL = (S_{IL}, \leq_{IL})$ is a lattice.

2. (30 points) The following system call adds read permission for a process (*for_pid*) if the caller (*call_pid*) owns the file, and does nothing otherwise. (The operating system supplies *call_pid*; the caller supplies the two latter parameters.)

```
function addread(call_pid , for_pid: process_id; fid: file_id): integer;
begin
    if (call_pid = filelist[fid].owner) then
        addright(filelist[fid].access_control_list , for_pid , "r");
        result := (call_pid - filelist[fid].owner);
        return result
    end .
```

- (a) Is the variable *result* directly or indirectly visible, or not visible?
 - (b) Is the variable *filelist*[*fid*].*owner* directly or indirectly visible, or not visible?
 - (c) Is the variable *filelist*[*fid*].*access_control* directly or indirectly visible, or not visible?
3. (40 points) Section 18.3.2.3 derives a formula for $I(A;X)$. Prove that this formula is a maximum with respect to p when $p = \frac{M^{\frac{1}{m}}}{1+mM^{\frac{1}{m}}}$, with M and m as defined in that section. (The value of p in the book is incorrect.)