

# January 12, 2024 Outline

**Reading:** *text*, §3.3–3.4

**Assignments:** Homework #1, due January 19; Project selection, due January 26

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## Module 7 (Reading: *text*, §3.3)

1. Take-Grant Protection Model
  - (a) Counterpoint to HRU result
  - (b) Symmetry of take and grant rights
  - (c) Islands (maximal subject-only *tg*-connected subgraphs)
  - (d) Bridges (as a combination of terminal and initial spans)

## Module 8 (Reading: *text*, §3.3.2–3.3.2)

2. Sharing
  - (a) Definition:  $\text{can}\bullet\text{share}(\alpha, \mathbf{x}, \mathbf{y}, G_0)$  true iff there exists a sequence of protection graphs  $G_0, \dots, G_n$  such that  $G_0 \vdash^* G_n$  using only take, grant, create, remove rules and in  $G_n$ , there is an edge from  $\mathbf{x}$  to  $\mathbf{y}$  labeled  $\alpha$
  - (b) Theorem:  $\text{can}\bullet\text{share}(\alpha, \mathbf{x}, \mathbf{y}, G_0)$  iff there is an edge from  $\mathbf{x}$  to  $\mathbf{y}$  labeled  $\alpha$ ; in  $G_0$ , or all of the following hold:
    - i. there is a vertex  $\mathbf{y}'$  with an edge from  $\mathbf{y}'$  to  $\mathbf{y}$  labeled  $\alpha$ ;
    - ii. there is a subject  $\mathbf{y}''$  which terminally spans to  $\mathbf{y}'$ , or  $\mathbf{y}'' = \mathbf{y}'$ ;
    - iii. there is a subject  $\mathbf{x}'$  which initially spans to  $\mathbf{x}$ , or  $\mathbf{x}' = \mathbf{x}$ ; and
    - iv. there is a sequence of islands  $I_1, \dots, I_n$  connected by bridges for which  $\mathbf{x}' \in I_1$  and  $\mathbf{y}' \in I_n$ .
3. Model Interpretation
  - (a) ACM very general, broadly applicable; Take-Grant more specific, can model fewer situations
  - (b) Example: shared buffer managed by trusted third party

## Module 9 (Reading: *text*, §3.3.3–3.3.4)

4.  $\text{can}\bullet\text{steal}(\alpha, \mathbf{x}, \mathbf{y}, G_0)$  definition and theorem
  - (a) Definition:  $\text{can}\bullet\text{steal}(\alpha, \mathbf{x}, \mathbf{y}, G_0)$  true iff there is no edge labeled  $\alpha$  from  $\mathbf{x}$  to  $\mathbf{y}$  in  $G_0$  and there exists a sequence of protection graphs  $G_0, \dots, G_n$  such that the following hold simultaneously:
    - i. there is an edge from  $\mathbf{x}$  to  $\mathbf{y}$  labeled  $r$  in  $G_n$ ;
    - ii. there is a sequence of rule applications  $\rho_1, \dots, \rho_n$  such that  $G_{i-1} \vdash^* G_i$  using  $\rho_i$ ; and
    - iii. for all vertices  $\mathbf{v}$  and  $\mathbf{w}$  in  $G_{i-1}$ ,  $1 \leq i < n$ , if there is an edge from  $\mathbf{v}$  to  $\mathbf{y}$  in  $G_0$  labeled  $\alpha$ , then  $\rho_i$  is *not* of the form “ $\mathbf{v}$  grants ( $\alpha$  to  $\mathbf{y}$ ) to  $\mathbf{w}$ ”.
  - (b) Theorem:  $\text{can}\bullet\text{steal}(\alpha, \mathbf{x}, \mathbf{y}, G_0)$  iff all of the following hold:
    - i. there is an edge from  $\mathbf{x}$  to  $\mathbf{y}$  labeled  $r$  in  $G_n$ ;
    - ii. there is a subject vertex  $\mathbf{x}'$  such that  $\mathbf{x}' = \mathbf{x}$  or  $\mathbf{x}'$  initially spans to  $\mathbf{x}$ ; and
    - iii. there is a vertex  $\mathbf{s}$  with an edge labeled  $\alpha$  to  $\mathbf{y}$  in  $G_0$  and for which  $\text{can}\bullet\text{share}(t, \mathbf{x}, \mathbf{s}, G_0)$  holds.
5. Conspiracy
  - (a) What is of interest?
  - (b) Access, deletion sets
  - (c) Conspiracy graph
  - (d) Number of conspirators

## Module 10 (Reading: *text*, §3.4)

6. Schematic Protection Model

- (a) Protection type, ticket, function, link predicate, filter function
- (b) Take-Grant as an instance of SPM